



# Study Of Geometrical Configuration Of Water Droplets

## Authors details

- 1- Muntaha Kaz (M.Sc.IV Sem Student, Department of Mathematics, Mohammad Ali Jauhar University, Rampur U.P.)
- 2- Swati Singh Rana (Associate Professor, Department of Mathematics, Mohammad Ali Jauhar University, Rampur U.P.)
- 3- Asha Bi  
(Assistant Professor (S.S.), Department of Physics, Mohammad Ali Jauhar University, Rampur U.P.)
- 4- Mohd. Akram (Assistant Professor, Department of Physics, Mohammad Ali Jauhar University, Rampur U.P.)

## Abstract

This research paper delves into the multifaceted realm of droplets, exploring their dynamic behaviour, diverse applications, and profound implications across various disciplines. The study begins by unravelling the intricate physics of droplet formation, considering fundamental factors such as surface tension, viscosity, and temperature. Investigating the biological landscape, the role of droplets in cellular processes and medical applications, such as drug delivery, is scrutinized. The atmospheric sciences section explores the formation of cloud droplets and rain, shedding light on the intricate interplay of aerosol particles and droplet dynamics. Microfluidics and lab-on-a-chip devices are gaining significant attention due to the pivotal role played by droplets in advancing healthcare, chemistry, and biology applications. From their impact on material properties to their relevance in energy harvesting and space environments, research in this field spans various frontiers of scientific and technological innovation. Additionally, studies are investigating droplet size analysis methods and their applications in industrial processes and environmental studies. As the paper progresses, it sheds light on the diverse contributions of droplets to fields such as food science, where they are integral to processes like emulsification, encapsulation, and the development of unique textures. The utilization of acoustic levitation to manipulate and control droplets presents intriguing possibilities in chemistry, physics, and medicine. Lastly, the paper delves into the intersection of droplets and environmental pollution, exploring the intricate ways in which droplets contribute to the transport and dispersion of pollutants in the atmosphere and water bodies. In summary, this research paper offers a comprehensive exploration of droplets, providing a nuanced understanding of their dynamics, applications, and broader implications in the realms of science and technology.

## **Keywords**

"Droplets", "Dynamic behavior", "Surface tension", "Viscosity", "Biological landscape", "Cellular processes", "Aerosol", "Emulsification", "Encapsulation", "Textures", "Acoustic levitation".

## **Introduction to Droplets [1]**

Droplets are diminutive, distinct entities of liquid or particles suspended in a gas, predominantly water droplets in the context of atmospheric science or technology. In meteorology, droplets play a pivotal role in the formation of clouds and precipitation. Water vapor in the atmosphere condenses into minuscule droplets, merging to form clouds, and eventually descending as rain or other forms of precipitation.

In the realm of technology, the term "droplet" is commonly linked with virtual servers in cloud computing. Digital droplets, also termed as cloud droplets or instances, are scalable and virtualized computing resources provided by cloud service providers. Droplets empower businesses and individuals to deploy, manage, and scale applications and services without the need for physical infrastructure. This holds true whether in the natural world or the digital domain, droplets epitomize the fundamental concept of small, discrete entities amalgamating to create a larger impact. Understanding the behaviour and characteristics of droplets is imperative in diverse fields, from weather prediction to contemporary computing architectures, underscoring their significance in shaping our comprehension of the physical and virtual realms.

## **Polymeric Surfactants as Emulsion Stabilizers [2]**

Droplet size and droplet size distribution play pivotal roles in characterizing emulsions, which are intricate mixtures of small liquid or particle units suspended in another substance, typically water droplets in atmospheric science or technology. Understanding and controlling these properties are essential for effectively utilizing or studying emulsions in various fields. There are several sophisticated techniques available to measure droplet size, including microscopy, laser diffraction, counting methods, sedimentation, and turbidity analysis.

In addition to the average droplet size, it is crucial to consider the droplet size distribution, which describes how the sizes of droplets are spread out within the emulsion. Emulsions with the same average droplet size but different distributions can exhibit vastly different behaviours. For instance, a truly monodisperse emulsion, characterized by uniformly sized droplets, would remain stable over time due to Ostwald ripening. This process involves larger droplets growing at the expense of smaller ones. Conversely, emulsions containing a diverse range of droplet sizes will evolve as smaller droplets disappear over time, leading to changes in their stability and rheological properties.

The rheological properties of emulsions, which describe how they flow and deform, are also greatly influenced by droplet size distribution. Generally, emulsions with smaller droplet sizes tend to be more stable, as reducing the average droplet size often enhances overall stability. However, there is a limit to this effect, as rapid Ostwald ripening can occur unless the dispersed phase is highly insoluble in the continuous phase.

Polymeric surfactants, molecules that aid in stabilizing emulsions by reducing surface tension at the interface between dispersed and continuous phases, can affect droplet size by influencing the emulsification process and overall stability. Their presence, enhancing emulsion stability, may also impact

droplet size. Comprehending these intricate dynamics is vital for optimizing emulsion properties across diverse applications, spanning from food and pharmaceuticals to cosmetics and industrial processes.

### **Wetting Characteristics of Surfaces [3]**

#### **Droplet Dimensions**

The significance of surface wetting characteristics remains paramount for applications involving self-cleaning surfaces. Typically, a hydrophobic wetting state is preferred due to the reduced adhesion between particles and the surface. This chapter introduces assessment mechanisms for the wetting state and presents relevant formulations for droplet contact angles. The Wenzel and Cassie-Baxter states are critically discussed, emphasizing their roles in self-cleaning applications. Droplet dimensions can be utilized to calculate the contact angle of a liquid droplet on a surface. In this scenario, specific measurement parameters are employed to determine the free surface profile of an axisymmetric droplet using the Laplace equation. The Laplace equation describes the profile of fluid interfaces and is given by:

$$\Delta P \gamma \left( \frac{1}{r_1} + \frac{1}{r_2} \right)$$

where  $r_1$  and  $r_2$  are the two principal radii of the free surface curvature, along with  $\Delta P$  representing the pressure difference across the interface, are essential components of this method. It utilizes mathematical expressions to predict small contact angles of a droplet, based on the radius of droplet curvature from an image and the droplet volume.

### **Water-Droplet Dynamics and Heat Transfer [4]**

Water droplets on inclined hydrophobic surfaces display varied dynamic behaviours when subjected to gravitational forces at different angles of inclination. Depending on the cohesion, resistance, and shear forces, droplets can either roll or slide on the surface, or they may become pinned. The primary forces governing droplet dynamics in terms of rolling and sliding are the droplet mass and the adhesion force exerted on the hydrophobic surface due to significant variations in droplet contact angle. Localized heating of the droplet induces Marangoni and buoyancy currents within the fluid, thereby influencing droplet dynamics on the hydrophobic surface. Surface texture parameters and the solid surface's free energy influence droplet contact angle and contact angle variation, leading to two potential states on the surface: the Wenzel state and the Cassie-Baxter state. Conversely, the adhesive force between the droplet and the solid surface is primarily determined by droplet contact angle variation, droplet size, and droplet fluid surface tension. Augmenting the contact angle variation enhances adhesion force, particularly noticeable for high-surface-tension fluids and large droplet diameters. Increased adhesion force at the droplet-solid interface significantly alters droplet dynamics, even leading to droplet adherence to the hydrophobic surface under substantial inclinations. Although surface inclination modifies the direction and magnitude of static force in a sessile droplet, the droplet remains adhered to the hydrophobic surface, and its initial shape deforms in response to force equilibrium. Geometric deformation of the droplet affects advancing and receding contact angles, thereby altering the adhesion force at the droplet-solid interface. Local heating induces fluid motion within the droplet, influencing its static behaviour and geometric features. Hence, investigating droplet pinning on inclined hydrophobic surfaces under localized heating conditions is crucial.

## Mathematical Modelling [5]

The internal fluidity of a resting droplet is simulated to match the experimental conditions of the slanted hydrophobic surface. These simulations consider linked flow and thermal fields simultaneously. The continuity equation for transient flow is:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho V) = 0 \quad (1)$$

where  $\rho$  is the water density,  $v$  is the liquid velocity.

For natural convection, density fluctuations are primarily caused by the thermal expansion of the fluid and can be described using Boussinesq's approximation as:

$$\rho = \rho_0 [1 - \beta(t - t_0)] \quad (2)$$

where  $\beta$  is known as the thermal expansion of the water and the momentum equation can be written as:

$$\rho \left( \frac{\partial v}{\partial t} + V \cdot \nabla v \right) = -\rho_0 \beta (T - T_0) \vec{g} - \nabla(p - p_0) + \nabla \left[ \mu (\nabla V + (\nabla V)^T) - \frac{2}{3} \mu (\nabla V) \right] \quad (3)$$

where  $p$  is the pressure,  $\mu$  is the dynamic viscosity of the liquid,  $g$  is the gravity and  $\rho_0$  is the hydrostatic pressure corresponding to density  $\rho_0$  and temperature to the flow. Field should satisfy the energy balance according to:

$$\rho C_p \frac{\partial T}{\partial t} + \rho C_p V \cdot \nabla T = \nabla \cdot (k \nabla T) \quad (4)$$

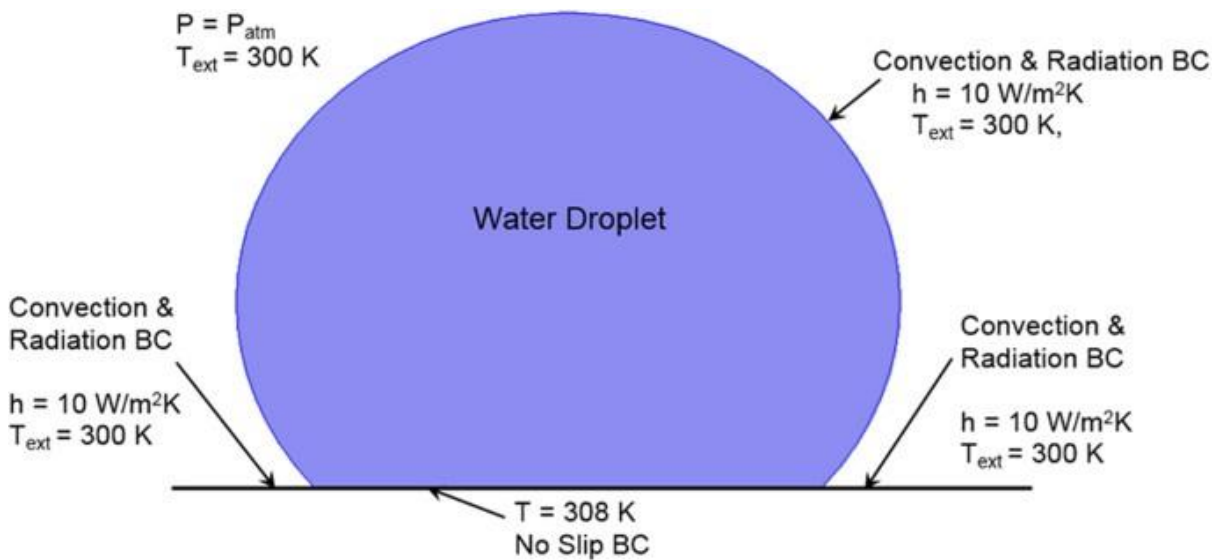
where  $C_p$  is the specific heat capacity and  $k$  is the thermal conductivity.

### Initial State

Initially, the droplet contains stagnant water. In this scenario, the flow velocity is set to zero, the pressure is set to the Laplace pressure, and the temperature is uniform, matching the ambient temperature (300 °K). The hydrophobic surface is maintained at 308 °K, aligning with experimental conditions.

### Boundary Conditions:

Figure 1 illustrates the boundary conditions utilized in the simulations. A constant pressure boundary is assumed at the droplet exterior, with the external pressure set at atmospheric pressure. Stagnant air surrounds the droplet's outer surface, resulting in zero air velocity. Natural convection ( $h = 10 \text{ W/m}^2\text{K}$ ) and radiation boundary conditions are applied at the interface between the droplet's free surface and its surrounding air, which is at a temperature of 300° K. Similarly, natural convection and radiation boundary conditions are applied to the free surface of the hydrophobic sample, not covered by the water droplet, i.e., at the hydrophobic surface exposed to ambient air. Since the hydrophobic surface remains at a constant temperature, a constant temperature boundary condition is employed at the interface between the droplet bottom and the hydrophobic surface. Furthermore, a non-slip boundary condition is applied at the interface between the droplet and the surface.



Due to the experiment's short duration and simulation timeframe, approximately 30 seconds, evaporation from the droplet surface is neglected in the simulations. This assumption is validated during the experiment, where droplet images are captured at 30 seconds and 100 seconds intervals and compared with the initial image. It is observed that the droplet dimensions remain identical in both images, justifying the exclusion of evaporation. Simulations are conducted with water droplet volumes of 10 $\mu$ L, 15 $\mu$ L, 20 $\mu$ L, and 25 $\mu$ L, while varying the inclination angle of the hydrophobic surface within the range of  $0^\circ \leq \delta \leq 180^\circ$ . A laminar two-phase flow moving mesh model coupled with heat transfer in the fluid model is employed. The models simultaneously solve numerically the continuity, momentum, and energy equations to obtain the flow field and temperature distribution. Performing three-dimensional simulations of the flow field and temperature distribution is resource-intensive due to excessive mesh requirements. Previous studies have shown that two-dimensional simulations yield very similar results compared to three-dimensional simulations. Therefore, two-dimensional simulation of the flow field is adopted.

In the numerical approach, finer meshes are concentrated in regions with high fluxes, and mesh independence tests are conducted for each droplet contact angle considered. The governing flow equations are discretized using the backward Euler finite difference method. An implicit scheme with a backward difference approximation ensures unconditionally stable solutions. The selection of the time step, crucial for accuracy, is set in the order of 10<sup>-4</sup> seconds. Residuals of flow parameters are monitored to assess convergence.

$$|\psi^k - \psi^{k-1}| \leq 10^{-8}$$

### **Physics of Droplet Formation [6]**

The intricate process of droplet formation is driven by a delicate interplay of forces, primarily dictated by surface tension. As a liquid stream undergoes stretching and thinning, it eventually reaches a critical point where surface tension induces the formation of a droplet. However, comprehending the underlying physics of this phenomenon requires a thorough investigation of the fluid dynamics involved.

Linear stability analysis provides valuable insights into estimating droplet dimensions. However, its limitations become apparent when attempting to capture the finer details of droplet structure, especially during the highly nonlinear pinch-off stage.

To delve deeper into this complex process, researchers have developed mathematical models based on asymptotic analysis, notably pioneered by Eggers and Dupont. These models leverage the Navier-Stokes equations to describe fluid flow, revealing a universal scaling that elucidates the self-similar nature of droplet formation.

Computational modelling serves as a cornerstone in simulating droplet creation, offering a platform to explore various scenarios and parameters. Finite difference and finite element methods are commonly employed to solve the mathematical equations governing droplet dynamics. In this context, the Portable, Extensible Toolkit for Scientific Computation (PET Sc) this approach arises as a significant asset for constructing dependable computational models.

Validation of these models is essential to ensure their accuracy and applicability. The Method of Manufactured Solutions (MMS) provides a rigorous framework for verifying computational code, while experimental investigations, such as those conducted by Zhang and Basaran, offer empirical validation.

These computational models are versatile, capable of simulating droplet formation across different liquids, including water, glycerol, and paraffin wax. By simulating pendant drops under various conditions, researchers aim to not only understand fundamental aspects of droplet formation but also extend their applicability to more complex pinch-off incidents.

In essence, the physics of droplet formation represents a fascinating yet intricate field of study, encompassing a broad spectrum of fluid dynamics and mathematical modelling techniques. Through a combination of theoretical analysis, computational simulations, and experimental validation, researchers strive to unravel the underlying mechanisms governing droplet formation in diverse scenarios.

## **Rheology of Emulsions [7]**

### **Droplets size**

Droplet dimensions in spherical-rigid type emulsions are typically within the range of 1 nm–50µm, with those falling between 1nm–1µm specifically termed as “colloidal.” Instead of relying solely on mean diameter, a particular emulsion's characterization is often enhanced by considering a range of droplet size distribution, where alterations in the sharpness or profile of the distribution curve over time serve as indicators of emulsion stability. Droplet size distribution also significantly impacts the viscosity of emulsions; viscosity tends to increase as droplet diameter decreases, particularly when electrostatic and steric interactions play significant roles. Moreover, viscosity tends to be higher when droplet size is relatively uniform, indicating a narrow distribution.

Determining droplet size distribution and diameter, particularly for larger droplets, can be achieved through optical microscopy. However, for smaller droplets, scanning electron microscopy (SEM) is more suitable, especially when examining frozen samples. Alternatively, in cases where emulsions are diluted, the dispersed liquid phase concentration is low, and droplet diameter is small, information about droplet size can be obtained through light propagation. When a light beam traverses through an emulsion, a portion of it is absorbed, another portion is reflected, and the remainder passes through. Many diluted fine emulsions exhibit turbidity, which is given as...

$$\frac{I_l}{I_0} = e^{-\tau l} \quad (1)$$

where  $I_l$  is the intensity of light passed through,  $I_0$  denotes the intensity of the incident light beam,  $\tau$  represents the turbidity, and  $l$  signifies the path length traversed through the sample droplet.

In accordance with Rayleigh's principle, the luminosity of the light ray traversing each droplet relies on the droplet's size and structure, as well as the discrepancy in refractive indices between the constituent liquid components. In the scenario of rigid spherical emulsions, the luminance  $I_d$  at a distance  $x$  from the droplet can be roughly approximated using the subsequent formula:

$$\frac{I_d}{I_0} \propto \frac{r^6}{r^2 \lambda^4} \quad (2)$$

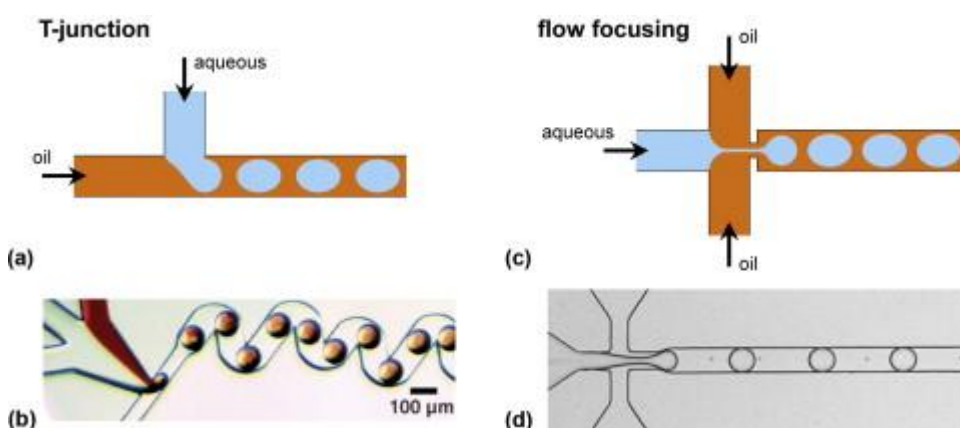
where  $\lambda$  is the wavelength and  $r$  are the droplet diameter.

Since the intensity of the light propagation is proportional to  $1/\lambda^4$ , blue light ( $\lambda = 450$  nm) propagates further than red light ( $\lambda = 650$  nm). If white light is used, then a diluted emulsion with droplet diameters in the range of 0.1–1  $\mu\text{m}$  will look bluish observed under the angle of 90 degrees with regard to the propagation beam. If the droplet diameter is smaller than 50 nm the emulsion will look transparent

## Microfluidics [8]

### **Droplet and Digital Microfluidics**

Droplet microfluidics has emerged as an exceptionally valuable tool for both chemical and biological procedures. This technique involves creating discrete volumes of a 'dispersed phase' solution within an immiscible 'continuous phase' liquid. Typically, this is achieved using devices featuring either a T-junction or a flow focusing layout (as depicted in Figure 1). By adjusting the surface characteristics of the microchannel and the flow rates of the immiscible solutions, it becomes feasible to produce various types of droplets, such as water-in-oil or oil-in-water, along with nested droplets. Additionally, microbubbles of gas can be generated using similar methodologies. These droplets can be generated at a remarkable pace, reaching hundreds or even thousands per second, and with exceptional reproducibility, thus serving as uniform reaction or analysis chambers. Moreover, multiple reagents can be introduced into these droplets and swiftly mixed within milliseconds. This versatile technique finds applications in diverse fields including particle synthesis, protein crystallization, polymerase chain reaction (PCR), and enzyme kinetics.



*Figure 1. Common chip designs for droplet generation: (a) T-junction generation, with (b) a photograph showing formation of the droplets in a fabricated device (reprinted from Song, H.; Bringer, M. R.; Tice, J. D.; Gerdt, C. J.; Ismagilov, R. F. *Appl. Phys. Lett.* **2003**, 83 (22), 4664–4666, with permission. Copyright 2003 American Institute of Physics). (c) Flow focusing generation, with (d) a photograph of droplet production.*

Digital Microfluidics employs droplets in a distinct manner. In this technique, the device comprises an array of electrodes covered with a hydrophobic insulator, onto which droplets can be deposited and subsequently manipulated through the application of electric fields (as illustrated in Figure 2). The movement of droplets can be precisely controlled, enabling tasks such as dispensing, merging, mixing, and separating. This level of control facilitates various applications including chemical reactions, extractions, and cell studies.

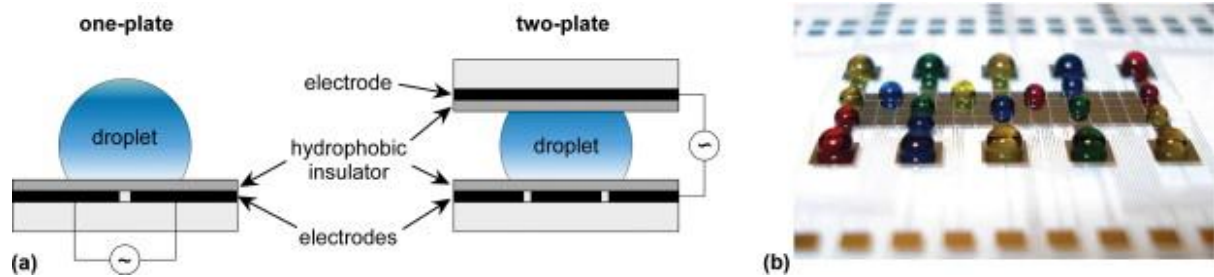


Figure 2. (a) One-plate and two-plate electrode arrays for digital microfluidics (redrawn from Jebrail, M. J.; Wheeler, A. R. *Curr. Opin. Chem. Biol.* **2010**, 14 (5), 574–581). (b) Photograph of an electrode array with multi-coloured droplets.

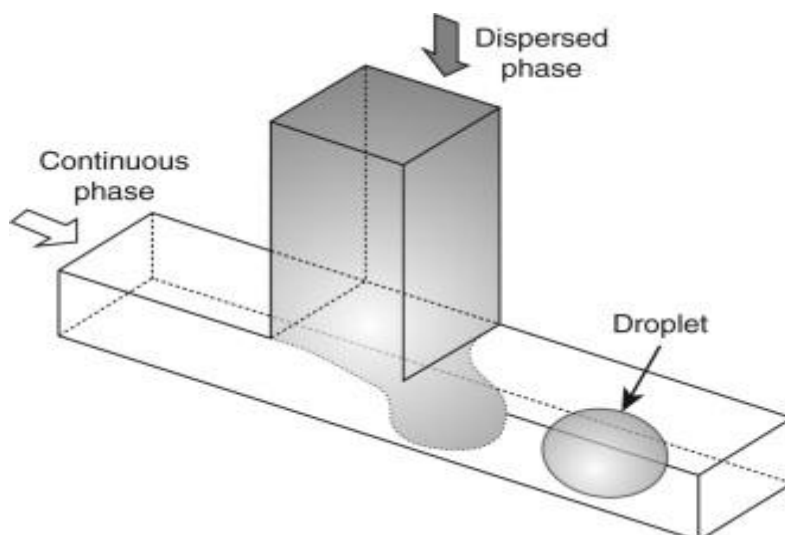
## Microfluidics: Technologies and Applications [9]

### Droplets Microfluidics

Droplet microfluidics, also known as digital microfluidics, is a subset of microfluidics that focuses on generating and manipulating discrete volumes of fluids within microdevices. Unlike continuous flow devices, which maintain a continuous flow of fluids, droplet microfluidics operates by creating discrete volumes using immiscible phases. These droplets are typically uniform in size, ranging from nanometres to micrometres in diameter. Each droplet can be independently controlled, serving as a microreactor that can be manipulated, transported, and subjected to various fluidic analyses.

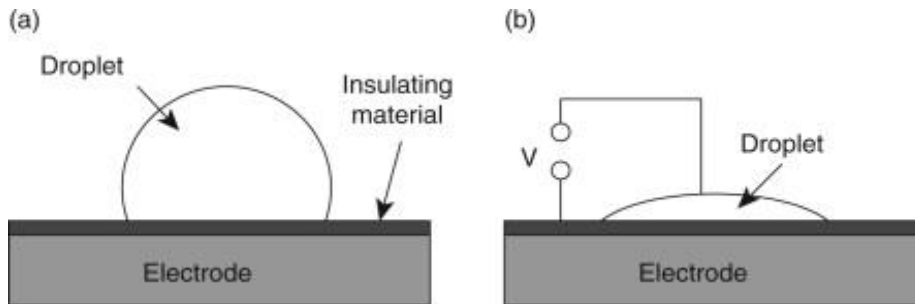
The ability to create and control numerous identical droplets or microreactors enables the execution of numerous parallel analyses and the collection of extensive datasets. This scalability is a key advantage of droplet microfluidic devices compared to continuous flow systems. Droplet microfluidics has found diverse applications in fields such as life sciences and chemistry, including DNA and protein analysis. Droplets can be generated by several different methods, such as those based on microfluidic channel geometry, electrical control among others. Geometry-based methods include microfluidic flow focusing and the use of a T-junction. The flow-focusing method involves the forced flow of a dispersed fluid and a continuous phase fluid through a narrow microfluidic structure, employing symmetric shearing of the dispersed phase by the continuous phase to generate droplets.<sup>18</sup> The T-junction method involves two immiscible fluids being brought together by means of a T-junction configuration of microfluidic channels with the inlet channel containing a dispersed phase fluid orthogonally intersecting a main channel containing a continuous phase fluid. Water is an example of a dispersed phase fluid and of a fluid to be dispersed. Oil is an example of a continuous phase fluid.

*Schematic of droplet generation by a T-junction consisting of microfluidic rectangular channels. The continuous phase fluid flows in the main channel and the fluid to be dispersed is supplied by the inlet. The diagram is not to scale.*



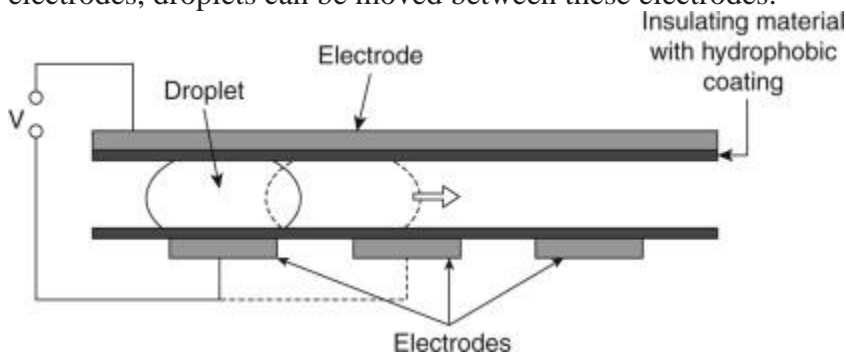


The manipulation of droplets involves various subcategories, encompassing overall motion, blending, division, and amalgamation. One strategy for blending, consolidating, and arranging droplets is through geometry-based pressure adjustment. Another method involves electrical manipulation techniques, such as electrowetting. Electrowetting on dielectric proves to be a viable technique for slicing, combining, generating, and transferring liquid droplets. Implementing methods like electrowetting to manipulate droplets can obviate the necessity for microfluidic components like pumps and valves. Electrowetting operates by regulating the surface's wetting properties through applied voltage. Aqueous droplets naturally assume a spherical bead shape on hydrophobic surfaces. Application of voltage between a droplet and an insulated electrode causes the droplet to spread on the electrode surface, owing to a reduction in the intersection angle amid the droplet and the substrate.



*Diagrammatic depiction of the electrowetting concept. (a) A fluid droplet on a water-repellent surface adopts an inherent spherical form. (b) The application of an electrical potential or voltage between the droplet and an electrode induces a decrease in the intersection angle between the droplet and the surface. This prompts the droplet to spread out and create a broader contact area on the surface. The illustration is not proportionally scaled.*

For droplet control or manipulation using the electrowetting on dielectric technique, electrical signals are utilized to control a sequence of electrodes positioned close to each other, determining the size and location of droplets. To exemplify, by sequentially applying or removing electrical signals to neighbouring electrodes, droplets can be moved between these electrodes.



*Schematic representation of the electrowetting on dielectric method for droplet actuation or motion. For droplet motion from left to right, an electric potential is applied between a droplet and an electrode at the bottom. Subsequently, this potential is removed and re-applied between an adjacent electrode and the droplet, shown by dotted lines. This causes the droplet to move from the first electrode toward the adjacent electrode. The diagram is not to scale.*

## **Hydrogels for Bioprinting [10]**

Exploring the vast landscape of bioprinting, we encounter a crucial element: hydrogels. These remarkable materials serve as the cornerstone for fabricating intricate tissue constructs with unparalleled biocompatibility. As we delve deeper into the intricacies of bioprinting, one undeniable truth emerges – the selection of bioink stands as a pivotal determinant of success. However, this journey extends beyond mere ink formulations; it necessitates tailoring these formulations to align seamlessly with the diverse array of bioprinting techniques at our disposal.

Within this chapter, we embark on a comprehensive exploration of hydrogels, focusing intently on their unique attributes and transformative applications within the realm of tissue engineering. Hydrogels, with their innate ability to mimic the intricate architecture of the extracellular matrix (ECM), provide an optimal

milieu for encapsulating cells and fostering their proliferation and differentiation. Yet, to harness the full potential of hydrogels in bioprinting, it is imperative to decipher the intricate interplay of factors governing the printability of bioink.

Our endeavour extends beyond mere exploration; it is a quest to unlock the secrets of gel-based bioprinting, transcending the barriers that stand in our path. Through innovative strategies and cutting-edge advancements in material science, we aim to surmount the inherent challenges, thereby propelling the frontiers of tissue engineering into uncharted territories.

Inspired by the seminal work of esteemed pioneers in the field, we seek to expand upon their foundational knowledge, breathing new life into the discourse surrounding hydrogel-based bioprinting. By unravelling the latest breakthroughs and emerging trends, we empower researchers and practitioners alike to push the boundaries of possibility in regenerative medicine and beyond.

### **Droplet-based bioprinting [11]**

Droplet-based bioprinting represents an advanced approach in which contact with the substrate is minimized. It entails the precise deposition of minute droplets containing bio-ink and cells onto predefined locations. Employing a multi-head system enables simultaneous printing of diverse bio-inks containing various cell types in controlled arrangements. This technique encompasses three primary systems: inkjet, microvalve-based jetting, and laser-assisted bioprinting. Inkjet systems, for instance, utilize thermal or piezoelectric forces to generate bubbles within bio-ink chambers, ejecting droplets onto surfaces at regular intervals. Such technology facilitates the direct printing of living cells with intricate patterns. However, a limitation lies in the challenge of creating 3D tissue or organ structures with adequate strength, primarily due to the use of low-viscosity bio-inks. Laser-assisted bioprinting, capable of handling thicker bio-inks, presents uncertainties regarding the effects of laser irradiation on cells. Moreover, laser-based systems tend to be more intricate and costly compared to inkjet or pneumatic pressure-assisted bioprinting methods.

### **Heat transfer during single droplet impact [12]**

In spray cooling applications, understanding the interaction between droplets and a heated substrate is crucial. This process is illustrated in the accompanying Figure, which depicts the behaviour of a single droplet impacting a solid surface. The graphical representation in Figure 9A demonstrates the intricate evolution of interface shape, temperature distribution, and pressure fluctuations during the collision of a solitary droplet with a heated superhydrophobic substrate. The dynamic sequence comprises distinct phases such as spreading, receding, and bounce-off, each offering significant insights into the underlying heat transfer mechanisms. To initiate the simulation, the entire computational domain is initially filled with air for a duration of 0.3 seconds, promoting the development of a thermal boundary layer that closely resembles real-world scenarios. Subsequently, the water droplet is introduced into the simulation, endowed with a specified impact velocity. Upon impact with the substrate, there is a noticeable increase in pressure in the vicinity of the wall region, indicating the localized dynamic response. Remarkably, the temperature contours reveal intriguing patterns, depicting lower temperatures at the precise location of the water droplet, juxtaposed against relatively higher temperatures observed within the surrounding air domain. This comprehensive analysis elucidates the complex interplay of variables governing droplet impact dynamics in the context of spray cooling applications.

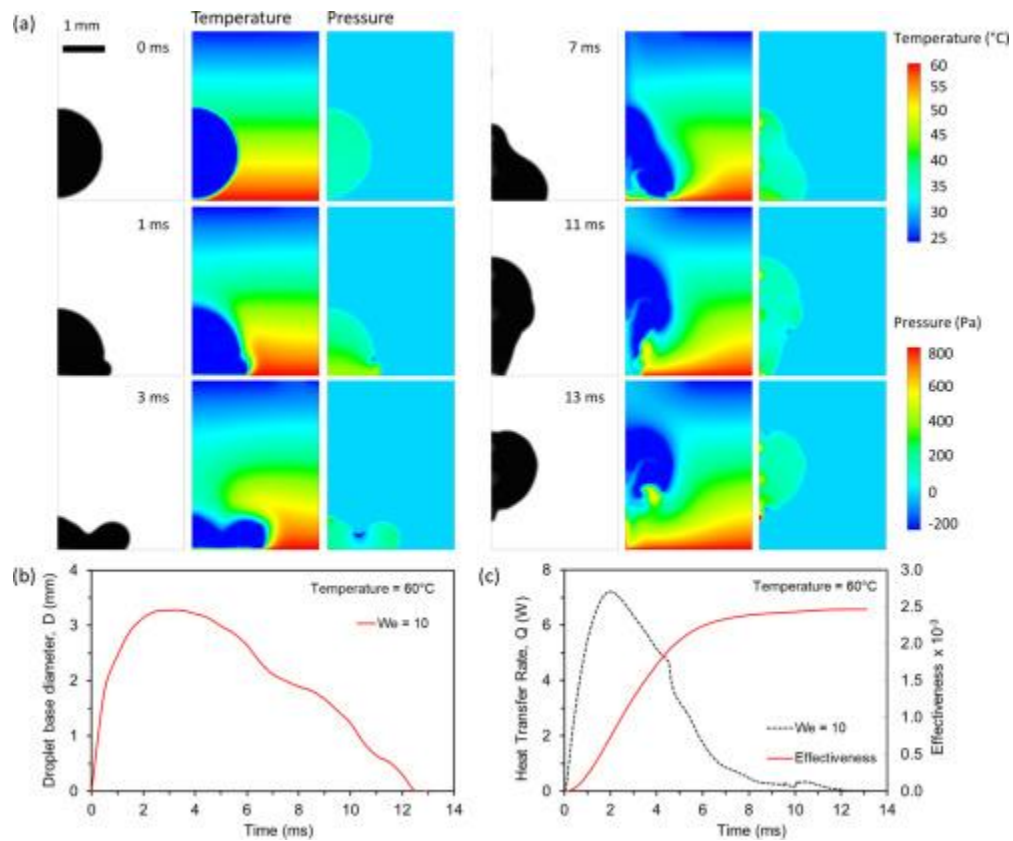


Fig. (A) Evolution of interfacial shape, temperature, and pressure contour during impact of single droplet on a heated superhydrophobic substrate with temperature of 40 °C. (B) base diameter (C) heat transfer rate (left) and cooling effectiveness (right) during the single droplet impact with  $We = 10$ .

The left axis of Figures B and C demonstrates the fluctuation of both droplet base diameter and heat transfer, respectively. It is observed that the droplet reaches its maximum spread diameter in approximately 3 milliseconds and rebounds in about 13 milliseconds. The heat transfer pattern closely mirrors the variation in droplet base diameter, as it is directly proportional to the wetted area of the droplet. During the spreading phase, there is a noticeable increase in heat transfer, which gradually decreases as the droplet recedes. This behaviour can be attributed to the wetting of the high-temperature substrate during the spreading phase, leading to the generation of a temperature gradient in the water domain near the wall. Conversely, during the receding phase, the temperature gradient near the wall region diminishes, accompanied by a reduction in the droplet's wetting area, resulting in lower heat transfer.

On the right side of the figure, the variation of cooling effectiveness over time is depicted. Notably, the cooling effectiveness increases steadily with time, albeit at a relatively slower rate during the receding phase due to the lower heat transfer.

In addition to the analysis of single droplet impacts, the literature discusses scenarios involving multiple droplets with simultaneous impact, as well as trains of droplets and other combinations. Despite advancements in understanding droplet impact phenomena, extrapolating this knowledge to spray cooling from such basic conditions presents significant challenges. Nonetheless, fundamental investigations remain essential as they offer a detailed examination of specific heat transfer mechanisms that are challenging to quantify in real-time spray cooling applications. Subsequent sections delve into the broader discussion surrounding the global performance of spray cooling mechanisms.

### Liquid droplets [13]

Liquid droplets play a pivotal role in numerous natural and industrial processes, their formation often occurring at the edges of cones due to the rupture of thin liquid films. This phenomenon, central to the study of fluid dynamics, finds applications across diverse fields, from environmental science to industrial engineering. Understanding the behaviour of liquid droplets are crucial for optimizing processes like spray cooling, inkjet printing, and combustion.

The intricate dynamics of liquid droplets are effectively captured through computational fluid dynamics (CFD) simulations, employing sophisticated techniques such as the Eulerian Wall Film (EWF) and Discrete Phase Model (DPM). These computational tools allow researchers to replicate droplet formation and track their trajectories in a Lagrangian reference frame. By integrating empirical data and theoretical models, CFD simulations provide valuable insights into droplet behaviour under various conditions.

In the realm of fluid dynamics, droplet formation is influenced by complex interactions between surface tension, fluid viscosity, and external forces such as gravity and shear. The velocity of the liquid film at the edges of cones dictates the flow rate of droplets, while drag forces from vapor flows affect their trajectories. Through advanced modelling techniques, researchers can quantify these interactions and predict droplet behaviour with remarkable accuracy.

One of the key advantages of employing CFD simulations is the ability to visualize droplet dynamics in intricate detail. By tracking droplets in the Lagrangian reference frame, researchers can observe their spatial distribution and temporal evolution in size. This level of detail enables the acquisition of quantitative data, essential for validating theoretical models and refining experimental designs.

Moreover, CFD simulations offer a versatile platform for investigating droplet behaviour across a wide range of scenarios. From studying droplet coalescence in cloud formation to optimizing spray cooling systems in industrial processes, the applications of CFD simulations are vast and diverse. By simulating droplet behaviour under different environmental conditions, researchers can gain insights into fundamental phenomena and develop strategies for mitigating potential risks.

The integration of empirical data and computational models enhances our understanding of droplet dynamics and facilitates the development of innovative solutions. For example, in the field of inkjet printing, optimizing droplet formation is essential for achieving high-resolution prints and minimizing ink wastage. By simulating the fluid dynamics within inkjet nozzles and printheads, researchers can refine printing parameters and enhance print quality.

Liquid droplets are integral to numerous natural and industrial processes, and understanding their behaviour is essential for optimizing performance and efficiency. Computational fluid dynamics (CFD) simulations provide a powerful tool for studying droplet dynamics, enabling researchers to replicate complex phenomena and gain valuable insights into fluid behaviour. By integrating empirical data and theoretical models, CFD simulations contribute to advancements in diverse fields, from environmental science to biomedical engineering, shaping the future of droplet research and technology.

In Figure 5, the left image depicts the distribution of liquid droplets in the Spinning Cone Column (SCC) as viewed from the z+ direction (looking down from the top). Heavy droplets are observed near the edge of the spinning cone, while finer droplets are present around the rotating shaft.

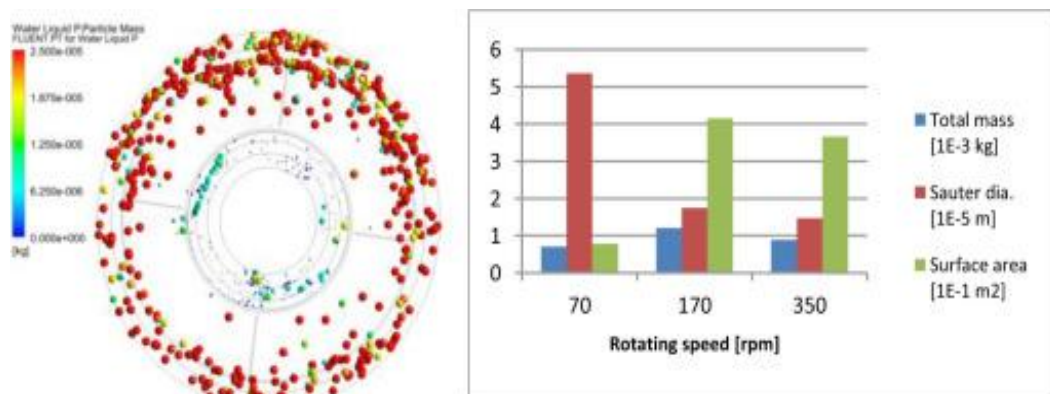


Figure Simulation results on liquid droplets (left-overall configuration, right-summary)

The plot on the right side of Figure 5 provides a comprehensive overview of the liquid droplets present in the Spinning Cone Column (SCC) at varying rotating speeds. An important observation derived from this summary is the estimated range of surface areas of droplets, which span from  $7.87\text{E-}02$  to  $4.15\text{E-}01$   $\text{m}^2$ . Notably, these values represent significant increases of 56% to 298% compared to the maximum area covered by the film in SCC. In essence, this implies that the removal rate of residual monomers could be substantially enhanced due to the notable expansion of the mass transfer area resulting from droplet formation.

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