



# The Essence of Mathematical Modeling: A Theoretical Exploration

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## **Abstract:**

Mathematical modelling constitutes a fundamental pillar of mathematics education, serving as a means of transforming real-world challenges into mathematical representations. This process entails the articulation of real-life scenarios into mathematical constructs, facilitating a bridge between tangible problems and abstract mathematical concepts. This approach underscores the pervasive role of mathematical models across various mathematical domains, encompassing arithmetic, algebra, geometry, and calculus.

As a consequence, mathematical modelling holds relevance for learners of all age groups, ranging from primary school to higher education. Recent examinations of the field emphasize the profound significance of modelling as an educational tool. Within this study, we aim to elucidate the significance, key attributes, and the procedural intricacies of mathematical modelling. It is important to note that this study is purely theoretical in nature and is envisioned as a valuable resource for future research endeavours.

## **Introduction:**

undertaken investigations focusing on the integration of mathematical modelling into In recent times, numerous researchers in the field of mathematics education have educational practices. The teaching and learning of modelling, along with its practical applications, encompass a multifaceted domain of mathematical thinking and the acquisition of mathematical skills (Burkhardt and Pollak, 2006; Niss, 1987, as cited by Mousoulides et al., 2005).

The motivation driving these inquiries within mathematics education stems from a dual concern: primarily, the essential query of "How can we equip students with mathematical knowledge and thinking skills that are applicable in real-life scenarios?" and subsequently, an confession come into view concerning the constraints innate in conventional teaching way and problem-solving guidance in terms of promoting students' problem-solving skills. (Kertil, 2008).

As Sağırılı (2010) has pointed out, a common question, particularly among students pursuing mathematics education or those from different academic disciplines, revolves around the relevance of mathematics in their lives (Özalp, 2006). This inquiry is entirely reasonable since, regrettably, mathematics is often perceived as an abstract, disconnected pursuit confined to the walls of educational institutions.

Nonetheless, the reality is quite different. Mathematics serves as a systematic mode of thought that generates solutions to real-life challenges and predicaments through the process of modelling (Niss, 1989). It stands as one of the most powerful tools for addressing real-world issues (Özalp, 2006). Consequently, mathematical modelling and its practical applications, as well as the methods for teaching and learning them, have become focal points of research across the globe. The overarching aim is to illustrate to students the integral role that mathematics plays in the real world (Kaiser et al., 2006).

In delving into the realm of mathematical modelling studies, it becomes evident that students can refine and reorganize their conceptual understanding through engagement with mathematical modelling techniques (Ottesen 2001; Lingefjard 2005). Furthermore, those who undergo mathematical modelling courses tend to exhibit higher proficiency in mathematical modelling skills (Keskin, 2008). Notably, mathematical modelling is predominantly employed in higher education settings, particularly in courses like analysis and linear algebra. Beyond its utility in academia, mathematical modeling's capacity to furnish real-life examples captivates students' interest in the subject matter.

Moreover, upon reviewing various research endeavours, a consistent consensus emerges favouring the integration of mathematical modelling into university curricula, often accompanied by concrete recommendations. Some investigations have also identified challenges encountered by students during the process of mathematical modelling; highlighting how these challenges can lead to deeper conceptual insights.

Additionally, the integration of technology in mathematical modelling applications has been explored in certain studies (Sağırılı, 2010). In contemporary times, there is an escalating demand for individuals who possess a synergy of technological proficiency across diverse fields such as engineering, architecture, economics, and technology. This necessitates honing problem-solving skills and fostering competence in mathematical modelling (Lingefjard, 2006).

Consequently, there exists a compelling mandate to nurture students' modelling skills by incorporating mathematical modelling approaches within mathematics education. The primary responsibility for accomplishing this task falls upon educators. If teachers themselves lack sufficient expertise in mathematical modelling and have not cultivated their modelling skills adequately, it stands to reason that students will encounter significant challenges in this educational endeavour (E. Bukova Güzel, I. Uğurel, 2010).

### **Diving into the World of Models and Modeling:**

While the terms 'model' and 'modelling' may appear commonplace, they encompass distinct connotations. 'Model' denotes the outcome of a modelling process, whereas 'modelling' pertains to the actual process itself. In essence, 'model' signifies the representation of tangible aspects of the physical world through meaningful symbols, aiming to simplify complexity. These models frequently surface in our daily lives when representing reality proves challenging or when direct access to reality remains constrained. For instance, an architect might showcase the features of a building intended for sale by crafting a model of the structure to be constructed. Fashion designers employ models to showcase their clothing creations, allowing others to appraise their designs. Children encounter miniature models of real-world objects (cars, trucks, trains, etc.) in their toys. Numerous such instances underscore the ubiquity of models in our daily existence. However, two common threads run through all these examples. Firstly, models serve the purpose of approximating or contemplating reality. Secondly, these models often present a simplified or idealized version of the subjects they represent (Lingefjard 2007; as cited by Sağırılı, 2010).

In the realm of mathematics education, one of the paramount objectives is to cultivate students' aptitude for mathematical thinking. This skill holds profound significance as it empowers students to decipher complex scenarios and devise solutions in problem-solving contexts. Consequently, emphasis must be placed on nurturing the mental models, diagrams, and concepts that students employ to interpret the problems they encounter and formulate solutions. A 'mathematical model' takes the form of a mathematical expression, be it a formula, equation, graph, or table, designed to encapsulate essential characteristics of a given situation. 'Mathematical modelling,' on the other hand, constitutes the process of constructing such mathematical models (The Consortium for Foundation Mathematics 2008). It is the art of transforming real-world situations into mathematical problems through the utilization of mathematical models. In essence, mathematical modelling is a distilled representation of the fundamental aspects of a real situation, achieved through the judicious application of mathematical symbols, relationships, and functions (Voskoglou 2006).

According to Galbraith and Clatworthy (1990), mathematical modelling entails the utilization of mathematics to solve unstructured problems within real-life contexts. In these modelling endeavours, mathematical methodologies are deployed to address real-world predicaments. The real-life issues encountered are transmuted into mathematical problems, subsequently tackled through mathematical techniques (Cheng, 2001).

As articulated by Gravemeijer, Stephan, and Cobb (2002), the genesis of models within the classroom is often a product of the informal activities engaged in by students. A pivotal milestone in the learning process involves the transition toward the development of mathematical models through real-life or problem-based scenarios. Only upon achieving this evolution can students effectively harness these models in their mathematical thought processes. It is essential to recognize that the notion of a mathematical model encompasses not only tangible structures like equations, functions, graphs but also mental representations and diagrammatic constructs. In essence, a mathematical model constitutes the amalgamation of these components, whether pre-existing or formulated subsequently, within our minds, with the purpose of mathematically representing a problem or real-life situation. Mathematical models serve as cognitive tools that equip individuals with the capacity to mathematically interpret the problems and circumstances they encounter (Kertil, 2008).

In the words of Berry and Houston (1995), mathematical modelling serves as a systematic approach for solving problems through mathematical means. A 'mathematical model,' by their definition, stands as a mathematical portrayal of the interrelationship between two or more variables pertinent to a given situation or problem. It is the aspiration of educators that students cultivate the skill of discovering mathematical models through their educational journey.

## **The Significance of Mathematical Modeling in Problem Solving**

In its most expansive scope, mathematical modelling entails the endeavour to mathematically elucidate a non-mathematical scenario, phenomenon, and the intricate connections among these scenarios, while uncovering mathematical patterns within them. This comprehensive definition, as articulated by Verschaffel, Greer, and De Corte (2002), encompasses the multifaceted processes of unraveling relationships, conducting mathematical analyses, deriving outcomes, and subsequently reinterpreting the model.

Lingefjard (2006) characterizes mathematical modelling as a dynamic process. Within this modelling process, there exists no rigid adherence to predefined rules when progressing from the given information towards the desired target. Instead, multiple trial-and-error procedures are typically employed between the initial data and the desired solution as an integral part of the modelling process (Lesh and Doerr, 2003).

The realm of mathematical modelling has increasingly captivated the attention of mathematics education researchers in recent years (Mousoulides et al., 2005). These studies on mathematical modelling encompass diverse theoretical underpinnings (Kaiser et al., 2006). As Kertil (2008) notes, while each modelling approach may diverge in terms of its definition, objectives, and curriculum implementation, some researchers view modelling as a pedagogical paradigm transcending constructivism in mathematics education. Conversely, others reduce mathematical modelling to the act of expressing real-life scenarios using mathematical language. Consequently, a standardized, universally accepted definition of mathematical modelling remains conspicuously absent in the academic literature.

According to Kaiser and Sriraman (2006), mathematical modelling enjoys widespread application in scientific and technological domains. They conceptualize mathematical modelling as a practical means of solving real-world problems, tethered to stringent real-life criteria. Drawing from years of research in the field, Lesh and Doerr (2003) present the model and modelling approach as an alternative to the constructivist approach in mathematics instruction. The model and modelling approach underscores that not all knowledge necessitates a structured process, with certain concepts, such as mathematical formulae and basic rules, existing at simpler knowledge levels that do not require structuring. This approach recognizes that among the various mental activities that transpire in the mind, such as classification and organization, structuring is but one facet. On a similar note, Greer, Verschaffel, and De Corte (2002) expound upon the application of mathematics in the form of mathematical modelling to address real-life problem situations. In contrast, Lehrer and Schauble distinguish between mathematical representation and modelling, advocating that mathematical representation and the exploration of relationships serve as a valuable starting point in the realm of mathematical modelling.

In a research study conducted by English and Watters (2004), they demonstrated that their modelling activities, undertaken with elementary-level students, had a more pronounced impact on the development of students' mathematical thinking and problem-solving skills compared to traditional problem-solving approaches. Furthermore, the findings from this study, which involved 3rd-grade elementary school students, underscored the potential to introduce advanced mathematical concepts and models to students at this level through mathematical modelling activities.

In the National Council of Teachers of Mathematics (NCTM) publication from 1999, it was emphasized that mathematical modelling stands apart from traditional problem-solving, despite sharing certain characteristics with various problem-solving definitions. The distinction lies in the process: situations in mathematical modelling must first be interpreted as problems, essential factors identified, relationships established, these relationships mathematically interpreted, opinions analyzed, and ultimately, solutions derived within the mathematical modelling framework.

### **Decoding the Steps of Mathematical Modeling**

Lesh and Doerr (2003) and Blum and Niss (1991) delineate problem-solving activities within the realm of mathematical modelling as a multifaceted process, comprising the following key stages:

a) **Understanding and Simplifying the Problem:** This entails comprehending the intricacies of the problem, interpreting information from sources such as tables, graphs, and verbal descriptions, and drawing meaningful inferences.

b) **Manipulating the Problem and Developing a Mathematical Model:** At this stage, the focus shifts towards identifying variables, elucidating the relationships between them, constructing hypotheses, evaluating contextual data, and ultimately constructing mathematical models that encapsulate the problem's essence.

c) **Interpreting the Shared Solution:** After formulating mathematical solutions, students proceed to make informed decisions, analyze the system, and propose potential resolutions.

d) **Verifying and Presenting the Problem:** This phase involves verifying the problem's solution, generalizing findings, and articulating solutions while examining them from various perspectives.

The process of mathematical modelling navigates between the realms of reality and mathematics. It commences with a complex real-life scenario, from which a problem representation is derived. Subsequently, the process entails mathematization to create a mathematical model. The solution is then sought through mathematical analysis of the model. The solution is first interpreted, and its validity is verified. If the solution or the chosen methodology doesn't align with reality, specific stages or the entire modelling process may be revisited and revised (Doruk, 2010).

The holistic modelling process offers numerous advantages:

- It provides students with experiential insight into how mathematics contributes to understanding, formalizing, and applying problems across various subjects.
- Students can apply models to define simple relationships in the natural world, gaining an appreciation of their potential and limitations.
- Students can engage in critical discussions regarding the applicability of existing models.
- The process enables students to seamlessly transition between theoretical and practical facets of modelling and mathematics-based problem-solving (Blomhøj and Kjeldsen, 2006).

Recent research in mathematics education underscores the need for more effective methods and strategies that engage all students in meaningful mathematical learning, fostering a sense that mathematics is integral to their lives and making mathematics enjoyable. Additionally, these methods must equip students with the skills to navigate the rapidly evolving technological landscape they will encounter in their professional lives. Moreover, there is a growing demand to ensure that students acquire mathematical competencies that empower them to efficiently navigate complex situations in their daily lives and devise practical solutions to everyday challenges.

In this context, modelling activities emerge as a highly effective tool that possesses the capacity to meet these multifaceted requirements, rendering them particularly suitable for integration into mathematics instruction by educators.

## REFERENCES

[1] Applied mathematical problem solving ,modelling ,application and links to other subjects-state trends and issues in mathematics instruction .Educational studies in mathematics, 22(1) ,37-68.

[2] Blum ,P., Galbraith, P.L., Henn, H., & Niss, m.(Eds). (2007). Modelling and applications in mathematics education: The 14<sup>th</sup> ICMI Study.

NEW YORK:Springer.

[3]Cheng, K.A. (2001). Teaching Mathematical Modelling in Singapore schools. The Mathematics Educator,6(1),62-74.

[4]Lesh,R., & Doerr, H.M.,(2003), Foundations of a Models and Modelling perspective on Mathematics Teaching, Learning, and Problem solving. In R.Lesh & H.M.Doerr (Eds) Beyond Constructivism : Models and Modelling Prospective on Mathematics Problem Solving , Learning &Teaching.

[5] Niss M., 1989 . Aims and Scope of Mathematical modelling in Mathematics Curriculum . Applications and Modelling in Learning and Teaching Mathematics .

