# INTERNATIONAL JOURNAL OF CREATIVE RESEARCH THOUGHTS (IJCRT) 

An International Dpen Access, Peer-reviewed, Refereed Journal

# Gourava Indices Of Product Graphs 

N.K.Raut<br>Ex-Head, Department of Physics, Sunderrao Solanke Mahavidyalaya Majalgaon Dist.Beed (India)


#### Abstract

First Gourava index is defined as $G O_{1}(G)=\sum_{u v \in E(G)}\left[d_{u}+d_{v}+d_{u} d_{v}\right]$, where $d_{u}$ is degree of vertex $u$. In this paper first Gourava index, second Gourava index, product connectivity Gourava index, sum connectivity Gourava index, first hyper Gourava index and second hyper Gourava index of tensor product, corona product and cartesian product of graphs are studied. KEYWORDS: Cartesian product, corona product, Gourava index, first hyper Gourava index, second hyper Gourava index, tensor product.


## I.INTRODUCTION

Let $\mathrm{G}=(\mathrm{V}, \mathrm{E})$ be a graph with order $|\mathrm{V}(\mathrm{G})|=\mathrm{n}$ and size $|\mathrm{E}(\mathrm{G})|=\mathrm{m}$. The degree of a vertex is denoted by $\mathrm{d}_{\mathrm{u}}$ and defined as the number of vertices adjacent to $u \in V(G)$. The edge connecting the vertices $u$ and $v$ is denoted by $u v$. All graphs considered here are finite, undirected and simple. In the field of graph theory, the graph operations produce new graph from initial ones. Binary operations create a graph from two initial graphs $\mathrm{G}_{1}\left(\mathrm{~V}_{1}, \mathrm{E}_{1}\right)$ and $\mathrm{G}_{2}\left(\mathrm{~V}_{2}, \mathrm{E}_{2}\right)$ such as graph union, graph intersection, graph join and graph products etc. Different versions of degree-based topological indices of molecular graphs are studied in [1-2]. Zagreb indices are widely studied in the literature for example [3-4]. There are several molecular graphs that can be realised as a product of graphs, for example nanotorus as $C_{n} \square C_{m}$, nanotubes as $\mathrm{P}_{\mathrm{n}} \square \mathrm{C}_{\mathrm{m}}$, grid as $\mathrm{P}_{\mathrm{n}} \square \mathrm{P}_{\mathrm{m}}$ [5]. R.P.Kumar et al. derived some topological indices of mesh, grid, torus and cylinder in [6]. W.Gao et al. studied multiple ABC index and multiple GA index of square grid [7].In [8] topological indices of grid are computed. Topological indices of graph product are studied in many papers [9-15]. Topological indices of graph operations are obtained in [16-18]. Figure for cartesian product of $\mathrm{P}_{4}$ and $\mathrm{P}_{6}$ is taken from [19] to study topological indices of family of Gourava index. Cartesian product of a cycle $C_{n}$ with a path $P_{m}$ is $P_{(n, m)}$ generalized prism graph with $|V|=m n$ and $|E|=n(2 m-1)[20-21]$. Weiner index and Hosaya polynomial of tubes and tori was studied by M.V.Diudea in 2005 [22]. Tensor product of two graphs $G_{1}$ and $G_{2}$ is the graph denoted by $\mathrm{G}_{1} \otimes \mathrm{G}_{2}$, with vertex set $\mathrm{V}\left(\mathrm{G}_{1} \otimes \mathrm{G}_{2}\right)=\mathrm{V}\left(\mathrm{G}_{1}\right) \times \mathrm{x}\left(\mathrm{G}_{2}\right)$, and any two of its vertices ( $\mathrm{u}_{1}, \mathrm{v}_{1}$ ) and ( $\mathrm{u}_{2}, \mathrm{v}_{2}$ ) are adjacent whenever $u_{1}$ is adjacent to $u_{2}$ in $G_{1}$ and $v_{1}$ is adjacent to $v_{2}$ in $G_{2}$ [23-24]. The corona product of two graphs $G$ and $H$ is defined as the graph obtained by taking one copy of $G$ and $|V(G)|$ copies of Hand joining the $i$-th vertex of $G$ to every vertex in the i -th copy of H . The corona product is denoted by $\mathrm{G} \odot \mathrm{H}$ [25-28]. Cartesian product of two graphs $\mathrm{G}_{1}=\left(\mathrm{V}_{1}, \mathrm{E}_{1}\right)$ and $\mathrm{G}_{2}\left(\mathrm{~V}_{2}, \mathrm{E}_{2}\right)$ denoted by $\mathrm{G}_{1} \mathrm{XG} \mathrm{G}_{2}$ or $\mathrm{G}_{1} \square \mathrm{G}_{2}$ containing vertex set $\mathrm{V}_{1} \mathrm{XV} V_{2}$ where ( $\mathrm{u}_{1}, \mathrm{u}_{2}$ ) is adjacent with ( $\mathrm{v}_{1}, \mathrm{v}_{2}$ ) iff where $\left[\mathrm{u}_{1}=\mathrm{u}_{2}\right.$ and $\mathrm{v}_{1}, \mathrm{v}_{2} \in \mathrm{E}_{2}$ ]or $\left[\mathrm{v}_{1}=\mathrm{v}_{2}\right.$ and $\mathrm{u}_{1} \mathrm{u}_{2} \in \mathrm{E}_{1}$ [29]. Gourava indices are degree-based indices defined in [30-35] as:

1) First Gourava index $=G O_{1}(G)=\sum_{u v \in E(G)}\left[d_{u}+d_{v}+d_{u} d_{v}\right]$.
2) Second Gourava index $=G O_{2}(G)=\sum_{u v \in E(G)}\left[\left(d_{u}+d_{v}\right) d_{u} d_{v}\right]$.
3) Product connectivity Gourava index $=P G O(G)=\sum_{u v \in E(G)} \frac{1}{\sqrt{\left(d_{u}+d_{v}\right\} d_{u} d_{v}}}$.
4) Sum connectivity Gourava index $=\operatorname{SGO}(G)=\sum_{u v \in E(G)} \frac{1}{\sqrt{\left(d_{u}+d_{v}\right\}+d_{u} d_{v}}}$.
5) First hyper Gourava index $=H G O_{1}(G)=\sum_{u v \in E(G)}\left[d_{u}+d_{v}+d_{u} d_{v}\right]^{2}$.
6) Second hyper Gourava index $=\operatorname{HGO}_{2}(G)=\sum_{u v \in E(G)}\left[\left(d_{u}+d_{v}\right)\left(d_{u} d_{v}\right)\right]^{2}$.

All the symbols and notations used in this paper are standard and mainly taken from books of graph theory [36-38]. In this paper first Gourava index, second Gourava index, product connectivity Gourava index, sum connectivity Gourava index, first hyper Gourava index and second hyper Gourava index of tensor product, corona product and cartesian product of graphs are studied.

## II.MATERIALS AND METHODS

A molecular graph is a simple graph related to the structure of a chemical compound. A molecular graph is constructed by representing each atom of a molecule by vertex and bonds between atoms by edges. In tensor product of two graphs we have, the vertex set $|V(G)|=n^{2}$ and edge set $|E(G)|=2(n-1)^{2}$ for $G=P_{4} \otimes P_{4}$. The corona product of two complete is denoted by $K_{n} \odot K_{m}$. The tensor product between $P_{4}$ and $P_{4}$, corona product between $K_{4}$ and $K_{3}$ and cartesian product of $\mathrm{P}_{4}$ and $\mathrm{P}_{4}$ are shown in figure 1,2 and 3 respectively. The edge partition represented for different product graph are in given table (1-3).

## III.RESULTS AND DISCUSSION

Let $G$ be a graph with $n$ vertices and $m$ edges. Different versions of Gourava index of product graphs are computed for path graphs and complete graphs. The edge partition of product graphs is considered for degree of end vertices. By graph operation a new graph is obtained. For these graphs the degree of end vertices is decided by observation and used in the computation of Gourava indices.

## Tensor product

Theorem 1.1: Let $P_{4}$ and $P_{4}$ be two path graphs.
Then first Gourava index of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}$ is $G O_{1}(G)=68+112(\mathrm{n}-3)+48(\mathrm{n}-3)^{2}$.
Proof. Partition the edge set $E(G)$ in four sets $E_{1}, E_{2}, E_{3}$ and $E_{4}$ as $\left|E_{14}\right|=4,\left|E_{22}\right|=4,\left|E_{24}\right|=8(n-3)$ and $\left|E_{44}\right|=2(n-$ $3)^{2}$ and using table (1).
Therefore $G O_{1}(G)=\sum_{u v \in E(G)}\left[d_{u}+d_{v}+d_{u} d_{v}\right]$

$$
\begin{aligned}
& =\sum_{14 \in E_{1}}[1+4+1 * 4]+\sum_{22 \in E_{2}}[2+2+2 * 2]+\sum_{24 \in E_{3}}[2+4+2 * 4]+\sum_{44 \in E_{4}}[4+4+4 * 4] \\
& =9 * 4+8 * 4+14 * 8(n-3)+48(n-3)^{2} \\
& =68+112(n-3)+48(n-3)^{2} \\
& \text { Theorem 1.2: Let } \mathrm{P}_{4} \text { and } \mathrm{P}_{4} \text { be two path graphs. }
\end{aligned}
$$

Then second Gourava index of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}$ is $G O_{2}(G)=144+384(\mathrm{n}-3)+256(\mathrm{n}-3)^{2}$.
Proof. Partition the edge set $\mathrm{E}(G)$ in four sets $\mathrm{E}_{1}, \mathrm{E}_{2}, \mathrm{E}_{3}$ and $\mathrm{E}_{4}$ as $\left|\mathrm{E}_{14}\right|=4,\left|\mathrm{E}_{22}\right|=4,\left|\mathrm{E}_{24}\right|=8(\mathrm{n}-3)$ and $\left|\mathrm{E}_{44}\right|=2(\mathrm{n}$ $3)^{2}$ and using table (1).
Therefore $G O_{2}(G)=\sum_{u v \in E(G)}\left[\left(d_{u}+d_{v}\right) d_{u} d_{v}\right]$
$=\sum_{14 \in E_{1}}[(1+4) 1 * 4]+\sum_{22 \in E_{2}}[(2+2) 2 * 2]+\sum_{24 \in E_{3}}[(2+4) 2 * 4]+\sum_{44 \in E_{4}}[(4+4) 4 * 4]$
$=20 * 4+16 * 4+48 * 8(n-3)+128 * 2(n-3)^{2}$
$=144+384(n-3)+256(n-3)^{2}$.
Theorem 1.3: Let $P_{4}$ and $P_{4}$ be two path graphs.
Then product connectivity Gourava index of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}$ is $P G O(G)=1.8944+\frac{8(n-3)}{\sqrt{48}}+\frac{2(n-3)^{2}}{\sqrt{128}}$.
Proof. Partition the edge set $\mathrm{E}(G)$ in four sets $\mathrm{E}_{1}, \mathrm{E}_{2}, \mathrm{E}_{3}$ and $\mathrm{E}_{4}$ as $\left|\mathrm{E}_{14}\right|=4,\left|\mathrm{E}_{22}\right|=4,\left|\mathrm{E}_{24}\right|=8(\mathrm{n}-3)$ and $\left|\mathrm{E}_{44}\right|=2(\mathrm{n}-$ $3)^{2}$ and using table (1).

Therefore $P G O(G)=\sum_{u v \in E(G)} \frac{1}{\sqrt{\left(d_{u}+d_{v}\right\} d_{u} d_{v}}}$
$=\sum_{14 \in E_{1}}\left[\frac{1}{\sqrt{[(1+4) 1 * 4]}}\right]+\sum_{22 \in E_{2}}\left[\frac{1}{\sqrt{[(2+2) 2 * 2]}}\right]+\sum_{24 \in E_{3}}\left[\frac{1}{\sqrt{[(2+4) 2 * 4]}}\right]+\sum_{44 \in E_{4}}\left[\left(\frac{1}{\sqrt{[(4+4) 4 * 4]}}\right]\right.$
$=\frac{4}{\sqrt{[5 * 4]}}+\frac{4}{\sqrt{[4 * 4]}}+\frac{8(n-3)}{\sqrt{[6 * 8]}}+\frac{2(n-3)^{2}}{\sqrt{[(1+4) 1 * 4]}}$
$=1.8944+\frac{8(n-3)}{\sqrt{48}}+\frac{2(n-3)^{2}}{\sqrt{128}}$.

Theorem 1.4: Sum connectivity Gourava index of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}=S G O(G)=4.1614+\frac{16(n-3)}{\sqrt{14}}+\frac{8(n-3)^{2}}{\sqrt{24}}$.
Theorem 1.5: First hyper Gourava index of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}=H G O_{1}(G)=580+1568(\mathrm{n}-3)+1152(\mathrm{n}-$ $3)^{2}$.

Theorem 1.6: Second hyper Gourava index of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}=\mathrm{HGO}_{2}(G)=2624+18432(\mathrm{n}-3)+$ 32768(n-3) ${ }^{2}$.

## Corona product

Theorem 2.1: Let $\mathrm{K}_{\mathrm{n}}$ and $\mathrm{K}_{\mathrm{m}}$ be two complete graphs with order n and m .
Then first Gourava index of corona product $\left(\mathrm{K}_{\mathrm{n}} \odot \mathrm{K}_{\mathrm{m}}\right)$ is $G O_{1}(G)=\mathrm{m}(2+\mathrm{m}) n^{m} C_{2}+\mathrm{nm}\left(m^{2}+n m+m+n-\right.$ 1) $+\left[2(n+m-1)+(n+m-1)^{2}\right]^{n} C_{2}$.

Proof. By using table (2), the edges for the corona product of complete graphs of order n and m on degree are $(m, m),(m, n+m-1)$ and $(n+m-1, n+m-1)$.

Therefore $G O_{1}(G)=\sum_{u v \in E(G)}\left[d_{u}+d_{v}+d_{u} d_{v}\right]$
$=\sum_{m m \in E_{1}}[m+m+m * m]+\sum_{m(n+m-1) \in E_{2}}[m+n+m-1+m(n+m-1)]+\sum_{(n+m-1)(n+m-1) \in E_{3}}[2(n+m-$ 1) $\left.+(n+m-1)^{2}\right]$
$=\mathrm{m}(2+\mathrm{m}) n^{m} C_{2}+\mathrm{nm}\left(m^{2}+n m+m+n-1\right)+\left[2(n+m-1)+(n+m-1)^{2}\right]^{n} C_{2}$.
Theorem 2.2; Let $K_{n}$ and $K_{m}$ be two complete graphs with order $n$ and $m$.
Then second Gourava index of corona product $\left(\mathrm{K}_{\mathrm{n}} \odot \mathrm{K}_{\mathrm{m}}\right)$ is
$G O_{2}(G)=\left(2 m^{3}\right) n^{m} C_{2}+(2 m+n-1)\left(m^{2}+n m-m\right) n m+2(n+m-1)^{3}\left({ }^{n} C_{2}\right)$.
Proof. By using table (2), the edges for the corona product of complete graphs of order $n$ and $m$ on degree are $(m, m),(m, n+m-1)$ and $(n+m-1, n+m-1)$.

Therefore $G O_{2}(G)=\sum_{u v \in E(G)}\left[\left(d_{u}+d_{v}\right) d_{u} d_{v}\right]$
$=\sum_{m m \in E_{1}}\left[(m+m) m^{2}\right]+\sum_{m(n+m-1) \in E_{2}}[(m+n+m-1) m(n+m-1)]+\sum_{(n+m-1)(n+m-1) \in E_{3}}[2(n+m-$ 1) $\left.(n+m-1)^{2}\right]$
$=\left(2 m^{3}\right) n^{m} C_{2}+(2 m+n-1)\left(m^{2}+n m-m\right) n m+2(n+m-1)^{3}\left({ }^{n} C_{2}\right)$.
Theorem 2.3: Let $K_{n}$ and $K_{m}$ be two complete graphs with order $n$ and $m$.
Then product connectivity Gourava index of corona product $\left(\mathrm{K}_{n} \odot K_{m}\right)$ is

$$
\operatorname{PGO}(G)=\frac{1}{\sqrt{2 m^{3}}} n^{m} C_{2}+\frac{n m}{\sqrt{(2 m+n-1)\left(m^{2}+n m-m\right)}}+\frac{1}{\sqrt{2(n+m-1)^{3}}}\left({ }^{n} C_{2}\right)
$$

Proof. By using table (2), the edges for the corona product of complete graphs of order $n$ and $m$ on degree are $(m, m),(m, n+m-1)$ and $(n+m-1, n+m-1)$.

Therefore $\operatorname{PGO}(G)=\sum_{u v \in E(G)} \frac{1}{\sqrt{\left(d_{u}+d_{v}\right\} d_{u} d_{v}}}$
$=\sum_{m m \in E_{1}} \frac{1}{\sqrt{(m+m) m^{2}}}+\sum_{m(n+m-1) \in E_{2}} \frac{1}{\sqrt{(m+n+m-1) m(n+m-1)}}+\sum_{(n+m-1)(n+m-1) \in E_{3}} \frac{1}{\sqrt{2(n+m-1)(n+m-1)^{2}}}$
$=\frac{1}{\sqrt{2 m^{3}}} n^{m} C_{2}+\frac{n m}{\sqrt{(2 m+n-1)\left(m^{2}+n m-m\right)}}+\frac{1}{\sqrt{2(n+m-1)^{3}}}\left({ }^{n} C_{2}\right)$.
Theorem 2.4: Sum connectivity Gourava index of corona product $\left(K_{n} \odot K_{m}\right)$ is $\frac{1}{\sqrt{2 m+m^{2}}} n^{m} C_{2}+$ $\frac{n m}{\sqrt{(2 m+n+m-1)+\left(m^{2}+n m-m\right)}}+\frac{1}{\sqrt{2(n+m-1)+(n+m-1)^{2}}}\left({ }^{n} C_{2}\right)$.
Theorem 2.5: First hyper Gourava index of corona product $\left(K_{n} \odot K_{m}\right)$ is $\left(2 m+m^{2}\right)^{2} n^{m} C_{2}+[(2 m+n-1)+$ $\left.\left(m^{2}+n m-m\right)\right]^{2} n m+\left[2(n+m-1)+(n+m-1)^{2}\right]^{2}\left({ }^{n} C_{2}\right)$.
Theorem 2.6: Second hyper Gourava index of corona product $\left(K_{n} \odot K_{m}\right)$ is $2 m^{3} n^{m} C_{2}+\left[(2 m+n-1)\left(m^{2}+\right.\right.$ $n m-m)]^{2} n m+\left[2(n+m-1)^{3}\right]^{2}\left({ }^{n} C_{2}\right)$.

## Cartesian product

Theorem 3.1: Let $\mathrm{P}_{4}$ and $\mathrm{P}_{4}$ be two path graphs.
Then first Gourava index of cartesian product $\mathrm{P}_{4} \square \mathrm{P}_{4}$ is $G O_{1}(G)=88+15(2 \mathrm{~m}+2 \mathrm{n}-12)+19(2 \mathrm{~m}+2 \mathrm{n}-8 \mathrm{n})+$ $24(2 n m-5 m-5 n+12)$.
Proof. Partition the edge set $E(G)$ in four sets $E_{1}, E_{2}, E_{3}$ and $E_{4}$ as $\left|E_{23}\right|=8,\left|E_{33}\right|=2 m+2 n-12,\left|E_{34}\right|=2 m+2 n-8$ and $\left|\mathrm{E}_{44}\right|=2 \mathrm{mn}-5 \mathrm{~m}-5 \mathrm{n}+12$, table (3).
Therefore $G O_{1}(G)=\sum_{u v \in E(G)}\left[d_{u}+d_{v}+d_{u} d_{v}\right]$
$=\sum_{23 \in E_{1}}[2+3+2 * 3]+\sum_{33 \in E_{2}}[3+3+3 * 3]+\sum_{34 \in E_{3}}[3+4+3 * 4]+\sum_{44 \in E_{4}}[4+4+4 * 4]$
$=88+15(2 m+2 n-12)+19(2 m+2 n-8 n)+24(2 n m-5 m-5 n+12)$.
Theorem 3.2: Let $P_{4}$ and $P_{4}$ be two path graphs.
Then second Gourava index of cartesian product $\mathrm{P}_{4} \square \mathrm{P}_{4}$ is $G O_{2}(G)=240+54(2 \mathrm{~m}+2 \mathrm{n}-12)+84(2 \mathrm{~m}+2 \mathrm{n}-$ $8)+128(2 n m-5 m-5 n+12)$.

Proof. Partition the edge set $E(G)$ in four sets $E_{1}, E_{2}, E_{3}$ and $E_{4}$ as $\left|E_{23}\right|=8,\left|E_{33}\right|=2 m+2 n-12,\left|E_{34}\right|=2 m+2 n-8$ and $\left|\mathrm{E}_{44}\right|=2 \mathrm{mn}-5 \mathrm{~m}-5 \mathrm{n}+12$, table (3).
Therefore $\mathrm{GO}_{2}(G)=\sum_{u v \in E(G)}\left[\left(d_{u}+d_{v}\right) d_{u} d_{v}\right]$
$=\sum_{23 \in E_{1}}[(2+3) 2 * 3]+\sum_{33 \in E_{2}}[(3+3) 3 * 3]+\sum_{34 \in E_{3}}[(3+4) 3 * 4]+\sum_{44 \in E_{4}}[(4+4) 4 * 4]$
$=240+54(2 m+2 n-12)+84(2 m+2 n-8)+128(2 n m-5 m-5 n+12)$.
Theorem 3.3: Let $P_{4}$ and $P_{4}$ be two path graphs.
Then product connectivity Gourava index of cartesian product $\mathrm{P}_{4} \square \mathrm{P}_{4}$ is $P G O(G)=1.46+\frac{2 m+2 n-12}{\sqrt{54}}+\frac{2 m+2 n-8}{\sqrt{84}}+$ $\frac{2 n m-5 m-5 n+12}{\sqrt{128}}$.
Proof. Partition the edge set $E(G)$ in four sets $E_{1}, E_{2}, E_{3}$ and $E_{4}$ as $\left|E_{23}\right|=8,\left|E_{33}\right|=2 m+2 n-12,\left|E_{34}\right|=2 m+2 n-8$ and $\left|\mathrm{E}_{44}\right|=2 \mathrm{mn}-5 \mathrm{~m}-5 \mathrm{n}+12$, table (3).
Therefore $\operatorname{PGO}(G)=\sum_{u v \in E(G)} \frac{1}{\sqrt{\left(d_{u}+d_{v}\right\} d_{u} d_{v}}}$
$=\sum_{23 \in E_{1}}\left[\frac{1}{\sqrt{[(2+3) 2 * 3]}}\right]+\sum_{33 \in E_{2}}\left[\frac{1}{\sqrt{[(3+3) 3 * 3]}}\right]+\sum_{34 \in E_{3}}\left[\frac{1}{\sqrt{[(3+4) 3 * 4]}}\right]+\sum_{44 \in E_{4}}\left[\left(\frac{1}{\sqrt{[(4+4) 4 * 4]}}\right]\right.$
$=1.46+\frac{2 m+2 n-12}{\sqrt{54}}+\frac{2 m+2 n-8}{\sqrt{84}}+\frac{2 n m-5 m-5 n+12}{\sqrt{128}}$.
Theorem 3.4: Sum connectivity Gourava index of cartesian product $\mathrm{P}_{4} \square \mathrm{P}_{4}=S G O(G)=2.421+\frac{(2 m+2 n-12)}{\sqrt{15}}+$ $\frac{(2 m+2 n-8)}{\sqrt{19}}+\frac{(2 n m-5 m-5 n+12)}{\sqrt{24}}$.
Theorem 3.5: First hyper Gourava index of cartesian product $\mathrm{P}_{4} \square \mathrm{P}_{4}=H G O_{1}(G)=968+225(2 \mathrm{~m}+2 \mathrm{n}-12)+$ $361(2 m+2 n-8)+16384(2 n m-5 m-5 n+12)$.
Theorem 3.6: Second hyper Gourava index of cartesian product $\mathrm{P}_{4} \square \mathrm{P}_{4}=\mathrm{HGO}_{2}(G)=7200+2916(2 \mathrm{~m}+2 \mathrm{n}-$ $12)+7056(2 m+2 n-8)+16384(2 n m-5 m-5 n+12)$.

| $\mathrm{d}_{\mathrm{u}}, \mathrm{d}_{\mathrm{v}}$ | 1,4 | 2,2 | 2,4 | 4,4 |
| :--- | :--- | :--- | :--- | :--- |
| Number of edges | 4 | 4 | $8(\mathrm{n}-3)$ | $2(\mathrm{n}-3)^{2}$ |

Table 1. Edge partition of tensor product $\mathrm{P}_{4} \otimes \mathrm{P}_{4}$.

| $\mathrm{d}_{\mathrm{u}}, \mathrm{d}_{\mathrm{v}}$ | $(\mathrm{m}, \mathrm{m})$ | $(\mathrm{m}, \mathrm{n}+\mathrm{m}-1)$ | $(\mathrm{n}+\mathrm{m}-1, \mathrm{n}+\mathrm{m}-1)$ |
| :--- | :--- | :--- | :--- |
| Number of edges | $\mathrm{n}^{\mathrm{m}} \mathrm{C}_{2}$ | nm | ${ }^{n} \mathrm{C}_{2}$ |

Table 2. Edge partition of corona product $K_{n} \odot K_{m}$.

| $m_{2,3}$ | $m_{3,3}$ | $m_{3,4}$ | $m_{4,4}$ |
| :---: | :---: | :---: | :---: |
| 8 | $2\left(n_{1}+n_{2}-6\right)$ | $2\left(n_{1}+n_{2}-4\right)$ | $2 n_{1} n_{2}-5 n_{1}-5 n_{2}+12$ |

Table 3. Edge partition of cartesian product $P n_{1} \square P n_{2}$.


Fig. 1. Tensor product of $P_{4}$ and $P_{4}$


Fig.2. Corona product $K_{4}$ and $K_{3}$


Fig.3. Cartesian product of $\mathbf{P}_{\mathbf{4}}$ and $\mathbf{P}_{\mathbf{4}}$.

## 4. Conclusion

Tensor product, corona product and cartesian product of different versions of Gourava index are obtained. If partition of edge set $\mathrm{E}(\mathrm{G})$ is known then the degree based topological indices and graph operations of any molecular graph can be computed.

## References

[1]S.Ediz,M.R.Farahani and M.Imran, On novel harmonic indices of certain nanotubes, International Journal of Advanced Biotechnology and Research,8(4) (2017) 277-282.
[2] N.K.Raut,G.K.Sanap, Different version of vertex degrees of molecular graph and topological indices, National Conference in Chemistry, Physics and Mathematics, International Journal of Scientific Research in Science and Technology,9(16) (2022) 178-184.
[3]M.Azari,A.Iranmanesh, Generalized Zagreb index of graphs, Studia Universitatis Babes-Bolyai,Chemia,56(3) (2011) 59-71.
[4]M.R.R.Kanna, S.Roopa and H.L.Parashivmurthy, Topological indices of Vitamin $D_{3}$, International Journal of Engineering and Technology,7(4) (2018) 6276-6284.
[5]P.Kandan, Status connectivity indices of cartesian product of graphs, TWMS J.App.Eng.Math.,9(4) (2019) 747754.
[6]R.P.Kumar,Soner Nandappa D. and M.R.R.Kanna, Computation of topological indices of mesh,grid,torus and cylinder, Applied Mathematical Sciences, 11(28) (2017)1353-1371.
[7]W.Gao,M.K.Siddiqui,M.Naeem and M.Imran, Computing multiple ABC and multiple GA index of some grid graphs, Open Physics, 16 (2018) 588-598.
[8]R.Kanabur, A study of topological indices of grid, International Journal of Advance Research in Science and Engineering,7(2) (2018)142-152.
[9]X.Wang, Z.Lin and L.Miao, Degree-based topological indices of product graphs,Open.J.Discret.Appl.Math.,4(3) (2021) 60-71.
[10]E.Sampathkumar, On tensor product graphs, Journal of the Australian Mathematical Society,1975,DOI:10.1017/514467887 00020619.
[11]B.N.Onagh, The harmonic index of product graphs,Math.sci.,11 (2017) 203-209.
[12]L.Deming, L.Mingju, Incidence colorings of cartesian products of graphs over path and cycles, Advances in Math.,40(6) (2021) 697-708.
[13]Sandi Klavazar, On the PI index; PI-partitions and cartesian product graphs, MATCH Commun.Math.Comput.Chem.,57(2007) 573-586.
[14]T.Selvi, Vaidhyanathan, On degree product of graphs, Int .J. of IT. Res. and Appli.,1(3) (2022) 6-10.
[15]K.Pittabiraman,S.Nagrajan and M.Chendrasekharan, Zagreb indices and coincides of product graphs, Journal of Prime Research in Mathematics, 10 (2015) 80-91.
[16]S,Sowmya, Sanskruti index of some graph operations, Pal Arch's Journal of Egypt,17(7) (2020) 1-7.
[17]B.S.Shwetha,V.Lokesha and P.S.Ranjini, On the harmonic index of graph operations,Trans.Combi.,4(4) (2015) 514.
[18]N.De, S.M.A.Nayeem and A.Pal, F-index of some graph operations, Mathematics Combinotorics,arXiv:1511.06661(math.CO),20 Nov 2015.
[19]A.Kaveh, H.Rahami, An efficient spectral method for bisection of regular finite element meshes, Asian Journal of Civil Engineering (Building and Housing),6(3) (2005) 127-143.
[20]M.Ajmal,W.Nazeer,M.Munir, S.M.Kang and C.Y.Jung, M-polynomials and topological indices of generalized prism network, International Journal of Mathematical Analysis, 11(6) (2017) 293-303.
[21]M.Cancan, S.Ediz, S.Fareed and M.R,Farahani, More topological indices of generalized prism network, Journal of Information and Optimization Sciences, 2020,DOI:10.1080/02522667.2020.1748273.
[22]M.V.Diudea, Distance counting in tubes and tori; Wiener index, Hosoya polynomial in nanostructures, Novel/Architecture, Nova, New York,2005,203-241.
[23]S.Maneka, R.S.Manikandan, The hyper Zagreb index of some product graphs, J.Math. Comput. Sci.,11(2) (2021) 1753-1766.
[24]U.P.Acharya, H.S,Mehata, 2-Tensor product of graphs, International Journal of Mathematics and Scientific Computing,4(1) (2014) 21-24.
[25]A.Khalid,N.Kausar,M.Munir,M.M.Al-Shamiri and T.Lamodaun, Topological indices of families of Bister and corona product of graphs, Journal of Mathematics, Hindawi, Volume 2022, Article ID 3567824.
[26]I.Yulliana, Dafik,I.H.Agustin and D.A.R.Wardani, On the power domination number of corona product and join graphs, IOP Con. Series Journal of Physics,Conf.Series, 1211 (2019)012020,1-10.
[27]K.Rajam,S.Monolisa and U.Mary, Topological descriptors for product of complete graphs, AIP Conference Proceedings,2261,030056(2020).
[28]D.Kumara,A.Mahasinge and H.Erandi, On the ABC and GA indices of the corona products of some graphs, Eurasian Chemical Communications, 3 (2021) 257-263.
[29]G.K.Jayanna, Reverse hyper Zagreb indices of the cartesian product of graphs,Int.J.Math.Combi.,4 (2021) 49-56.
[30]V.R.Kulli, The Gourava indices and coincides of graphs, Annals of Pure and Applied Mathematics,14(1) (2017) 33-38.
[31]V.R.Kulli, The product connectivity Gourava index, Journal of Computer and Mathematical Sciences,8(6) (2017) 235-242.
[32]V.R.Kulli, On the sum connectivity Gourava index, International Journal of Mathematical Archive,8(6) (2017) 211-217.
[33]V.R.Kulli, On hyper Gourava indices and coincides, International Journal of Mathematical archive,89(12) (2017) 116-120.
[34]S.Kanwal,A.Riasat,M.K.Siddiqi,S.Malik,K.Sarwar,A.Ammara and A.T.Anton, On topological indices of total graph and its line graph for Kragujevac tree networks, Hindawi, Complexity, Volume 2021,Article ID8695121,32pages.
[35]B.Basavanagoud, S.Policepatil, Chemical applicability of Gourava and hyper-Gourava indices,Nanosystems:Physics,Chemistry,Mathematics,12(2) (2021) 142-150.
[36]N.Deo,W.Imrich and S.Klavzar, Product graphs, Structure and Recognition, (John Wiley) New York,(2000). Graph Theory, Prentice-Hall of India, Private Ltd., 2007, New Delhi.
[37]F.Harary, Graph Theory, Narosa Publishing House, New Delhi, 1969.
[38]N.Trinajstić, Chemical Graph Theory, CRC Press, Boca Raton, FL.,1992.

