



Mathematical Model Of Extracting The Negative Phase Sequence Components From Three-Phase Alternating Current Using A Numerical Relay Algorithm

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ABSTRACT

An issue that has been plaguing protection engineers for a considerable amount of time is the extraction of negative phase sequence components from three-phase alternating current voltages and currents. In this research, a unique numerical three-phase filtering approach is presented for the purpose of extracting the negative phase sequence components from sampled three-phase observations. In order to calculate either the absolute value of the negative phase quantity or the relative value of the negative phase sequence to the positive phase sequence measured at the operating point, the mathematical algorithm has been designed to be appropriate for use in a numeric relay. This is because the method has been developed to be suitable for use in its intended application. The purpose of this study is to illustrate the capabilities of the method by presenting findings that indicate that the amount of negative phase sequence components can often be retrieved within thirty milliseconds after a disturbance by using a simple post-extraction smoothing filter. A notional sampling rate of 1200 samples per second was used in this example, together with an automated frequency tracking method, in order to ensure that the sampling clock and the power system frequency remained in perfect sync with one another.

Key words: Mathematical model, Relay algorithm, AC, Negative phase sequence.

I. INTRODUCTION

The presence of negative phase sequence components in the current or voltage signals of a three-phase system might indicate that the system is either faulty or that it is being operated in an abnormal condition. In the case of power transformers, motors, and generators, the existence of negative phase sequence components always results in overheating. In an ideal scenario, this overheating leads to protective tripping, which isolates the plant in question from the rest of the power supply network. When it comes to collecting negative phase sequence components, the conventional methods include the use of specific hardware filters that contain phase shifting components. The majority of the time, they are connected to electromechanical relays and early static designs.

Figure 1 depicts a design that is more advanced [1] and that has the ability to circumvent this issue. For the sole purpose of determining the value of the negative phase sequence current, this makes use of the three phase electrical currents. Both of these methods are vulnerable to fluctuations in the frequency of the power system to which they are sent. This technique enabled improved phase shifting and mixing circuits, which resulted in more effective filters. Similar negative phase sequence filters were created for the analogue static relays. However, this technology was more effective than the alternatives.

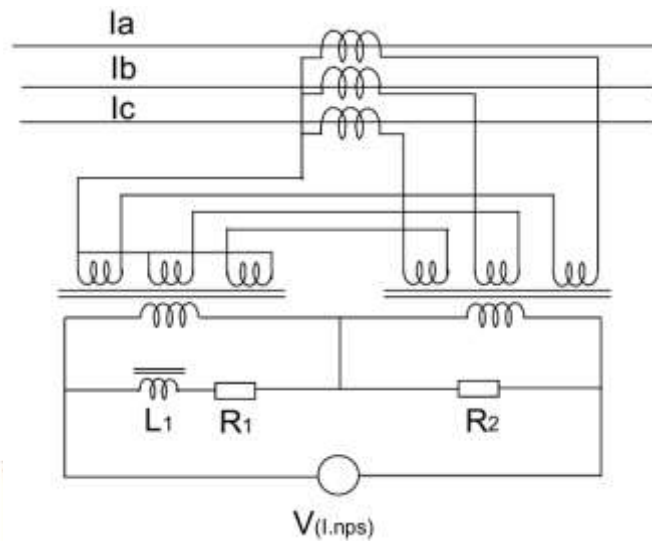


Figure 1. Practical Negative Phase Sequence Current Filter

The development of general-purpose microprocessor relay platforms has resulted in the use of processors that are ever more powerful, as well as the implementation of numerical relaying algorithms with increasing frequency. The equation that is used to determine the negative phase sequence current I_2 is as follows:

$$I_2 = \frac{1}{3}(I_a \angle 0 + a^2 I_b \angle \theta_b + a I_c \angle \theta_c) \quad (1).$$

Simple algebraic manipulation then yields:-

$$I_{r2} = \frac{1}{3}(I_{ra} - 0.5 I_{rb} - 0.5 I_{rc} + \frac{\sqrt{3}}{2} I_{xb} - \frac{\sqrt{3}}{2} I_{xc}) \quad (2).$$

$$I_{x2} = \frac{1}{3}(-\frac{\sqrt{3}}{2} I_{rb} + \frac{\sqrt{3}}{2} I_{rc} - 0.5 I_{xb} - 0.5 I_{xc}) \quad (3).$$

and,

$$|I_2| = \sqrt{I_{r2}^2 + I_{x2}^2} \quad (4).$$

where:-

I_2 is the negative phase sequence current

I_{r2} and I_{x2} are the real and quadrature components of I_2

I_a , I_b and I_c are the three phase currents

I_{ra} , I_{rb} and I_{rc} and I_{xa} , I_{xb} and I_{xc} are the real and quadrature components of the three phase currents

An innovative sampling and time-multiplexed phase-sensitive rectification approach to ascertain the values of I_{ra} , I_{rb} , I_{rc} , I_{xa} , I_{xb} , and I_{xc} , therefore facilitating the determination of I_2 . This circumvents complex signal processing, hence reducing the demands on the relay's CPU.

II. THE NEGATIVE PHASE SEQUENCE ALGORITHM.

The newly developed technique employs a numeric filter consisting of three phases for the purpose of addressing negative phase sequence. The instantaneous power equation and the Fourier series filter are both integral to the operation of this system. The Fourier series filter is fundamental to its operation. The system has been designed for implementation within the digital signal processing framework of a modern protection relay platform, utilizing a moderate sampling rate and sampling points that are automatically synchronized to the frequency of the power system.

Using the separate instantaneous values of the voltage and current measurements, the instantaneous power equation is able to calculate a direct current value of the instantaneous three-phase power in a circuit. -!

$$P = i_a v_a + i_b v_b + i_c v_c = IV \cos(\theta) \quad (5).$$

This can be presented more generally as:-

$$S_R = s_a \sin(\omega t) + s_b \sin\left(\omega t + \frac{2\pi}{3}\right) + s_c \sin\left(\omega t + \frac{4\pi}{3}\right)$$

$$S_R = S \cos(\theta) \quad (6).$$

This represents the real part of the signal S and the quadrature term can be derived from:-

$$S_X = s_a \cos(\omega t) + s_b \cos\left(\omega t + \frac{2\pi}{3}\right) + s_c \cos\left(\omega t + \frac{4\pi}{3}\right)$$

$$S_X = S \sin(\theta) \quad (7).$$

The magnitude of signal S is derived from:-

$$|S| = \sqrt{S_R^2 + S_X^2} \quad (8).$$

This presumes that the input phasor set, S_a , S_b , and S_c , comprises three-phase signals rotating in synchrony with the reference phasors $\sin(\omega t)$, $\sin(\omega t + 2\pi/3)$, and $\sin(\omega t + 4\pi/3)$, all possessing unit magnitude. Recognizing the improbability of balanced input phasors being in synchronism with the reference phasor set, filtering is used to focus on the power frequency component and remove components that do not rotate in synchronism with the reference phasors.

In this generalized formula, S_a , S_b , and S_c represent sampled three-phase current signals, whereas $\sin(\omega t)$, $\sin(\omega t + 2\pi/3)$, and $\sin(\omega t + 4\pi/3)$ constitute a three-phase set of unit magnitude reference phasors. S denotes the positive phase sequence current.

For the balanced components, the designations S_R and S_X are essentially direct current. Imbalanced elements in the input phasors produce sinusoidal signals at the power system frequency or its second harmonic. Numerous filtering approaches exist for the extraction of these DC components, and several windowing procedures have been examined. The extraction methods for the aforementioned are represented as follows:

$$S_{DR} = \frac{1}{N} \sum_{n=-N}^{n=0} f_n (s_{an} \sin(wn) + s_{bn} \sin\left(wn + \frac{2\pi}{3}\right) + s_{cn} \sin\left(wn + \frac{4\pi}{3}\right))$$

$$S_{DX} = \frac{1}{N} \sum_{n=-N}^{n=0} f_n (s_{an} \cos(wn) + s_{bn} \cos\left(wn + \frac{2\pi}{3}\right) + s_{cn} \cos\left(wn + \frac{4\pi}{3}\right))$$

and;-

$$|S_D| = \sqrt{S_{DR}^2 + S_{DX}^2} \quad (9).$$

where:-

S_{DR} and S_{DX} are the derived real and quadrature values for S_D n is the sample, N is window length, F_n is the window function.

The window length is an integer multiple of power system frequency cycles, influencing the algorithm's reaction speed and the filter's frequency selectivity. The technique defined in equation (9) employs a positive rotating set of reference phasors, hence facilitating the extraction of the positive phase sequence components of S_a , S_b , and S_c . To extract the negative phase sequence components, a collection of negative rotating reference phasors is needed, namely:

$\sin(wt)$, $\sin(wt+4\pi/3)$ and $\sin(wt+2\pi/3)$

The negative phase sequence extraction algorithm is:-

$$N_{DR} = \frac{1}{N} \sum_{n=-N}^{n=0} f_n (s_{an} \sin(wn) + s_{bn} \sin\left(wn + \frac{4\pi}{3}\right) + s_{cn} \sin\left(wn + \frac{2\pi}{3}\right))$$

$$N_{DX} = \frac{1}{N} \sum_{n=-N}^{n=0} f_n (s_{an} \cos(wn) + s_{bn} \cos\left(wn + \frac{4\pi}{3}\right) + s_{cn} \cos\left(wn + \frac{2\pi}{3}\right))$$

and;-

$$|N_D| = \sqrt{N_{DR}^2 + N_{DX}^2} \quad (10).$$

The zero phase sequence components are extracted in a similar manner using a static set of reference phasors i.e.:-

$\sin(wt)$, $\sin(wt)$ and $\sin(wt)$

It is possible to deconstruct the zero phase sequence extraction method into the following:

$$Z_{DR} = \frac{1}{N} \sum_{n=-N}^{n=0} f_n (s_{an} + s_{bn} + s_{cn}) \sin(wn)$$

$$Z_{DX} = \frac{1}{N} \sum_{n=-N}^{n=0} f_n (s_{an} + s_{bn} + s_{cn}) \cos(wn)$$

$$|Z_D| = \sqrt{Z_{DR}^2 + Z_{DX}^2} \quad (11).$$

III. SIMULATION STUDIES.

Simulations were conducted using MATLAB, resulting in the development of a model representing an ideal three-phase synchronous generator supplying a balanced load via a feeder network. To demonstrate the functionality of the negative phase sequence algorithm, various scenarios involving short circuit faults and broken wire conditions were analyzed. Figure 2 illustrates the effects observed when a single phase to ground fault is applied to the generator's connections following a duration of 0.1 seconds. Subsequent to the fault occurrence, the program identifies the new number within a time frame of less than 36 milliseconds.

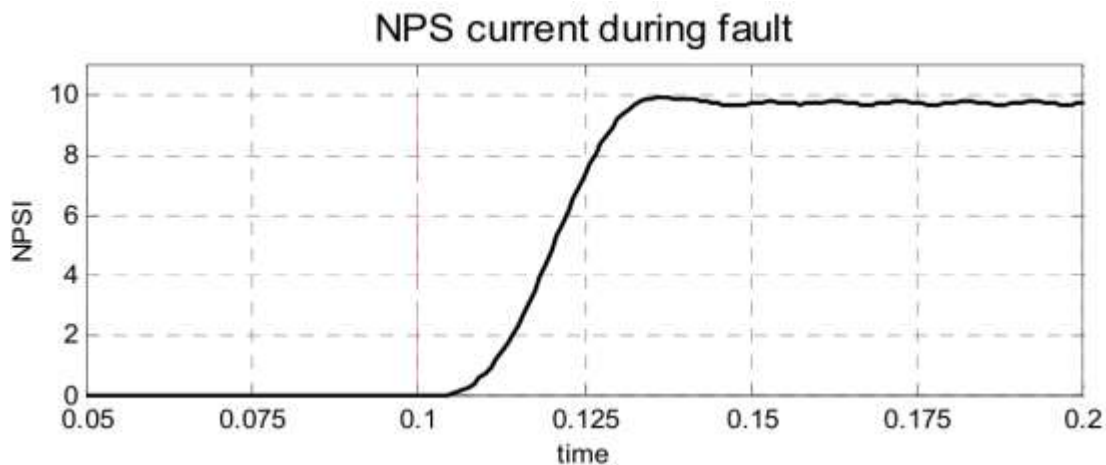


Figure 2. Single Phase to Ground Fault at the Generator Terminals

If there was a phase-to-phase fault on the generator's inputs, the reaction was the same, as shown in Figure 3.

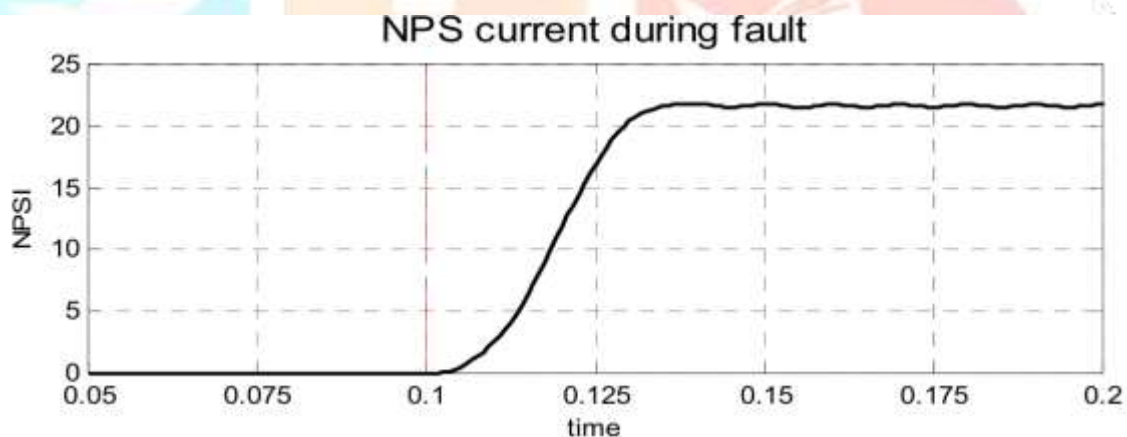


Figure 3. Phase to Phase Fault at the Generator Terminals

During the occurrence of a three-phase fault at the generator terminals, the response indicated that within the data capture period of the algorithm, corresponding to the duration of the window, a negative phase sequence component was identified. The use of the filter output without additional processing may lead to confusion. Implementing a 30 to 40 ms check on the output will ensure that transients of this nature do not result in undesirable tripping, thereby resolving the issue. This will, naturally, extend the duration of the transfer process and prolong the decision-making time for the trip. Figure 4 illustrates the procedure for rectifying this fault.

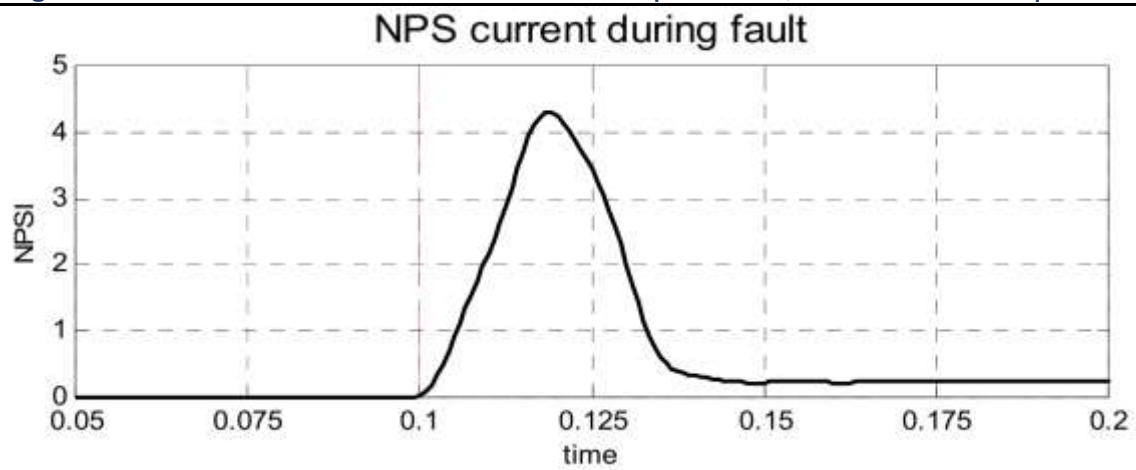


Figure 4. Three-Phase Fault at the Generator Terminals

The successful removal of a phase-to-phase fault is shown in Figure 5. The fault is put in place after 0.1 seconds and taken away after 0.15 seconds.

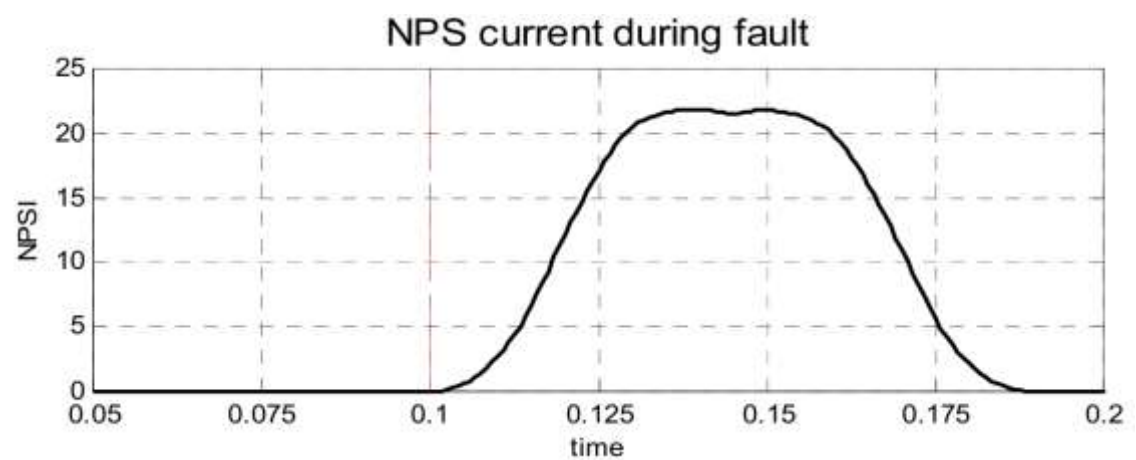


Figure 5. Phase to Phase Fault at the Generator Terminals cleared after 50 ms

A load that isn't balanced is shown in Figure 6, which looks at what happens when one part of the load is lost.

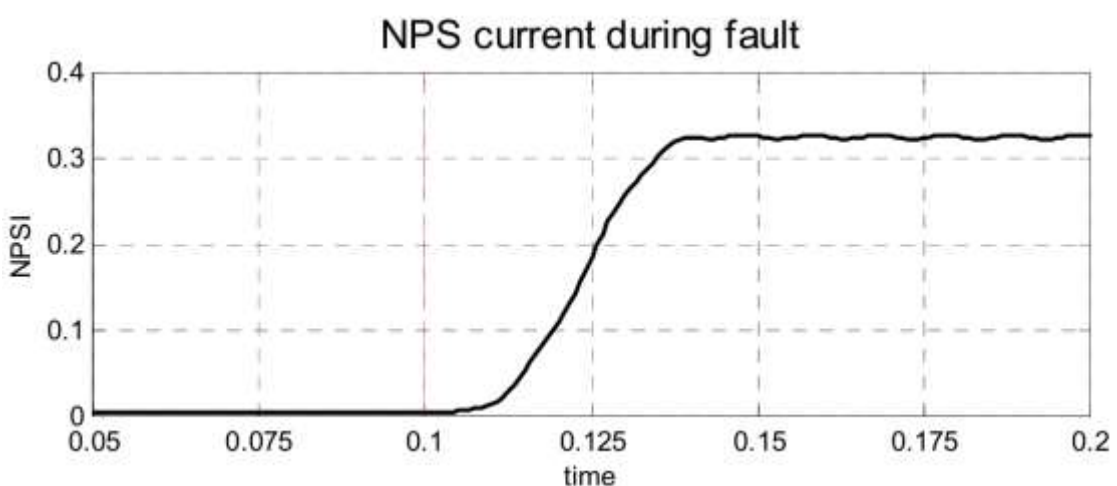


Figure 6. Loss of One Phase of the Load on the Generator

Figure 7 illustrates the reaction that transpired as a result of the loss of two phases of the load.

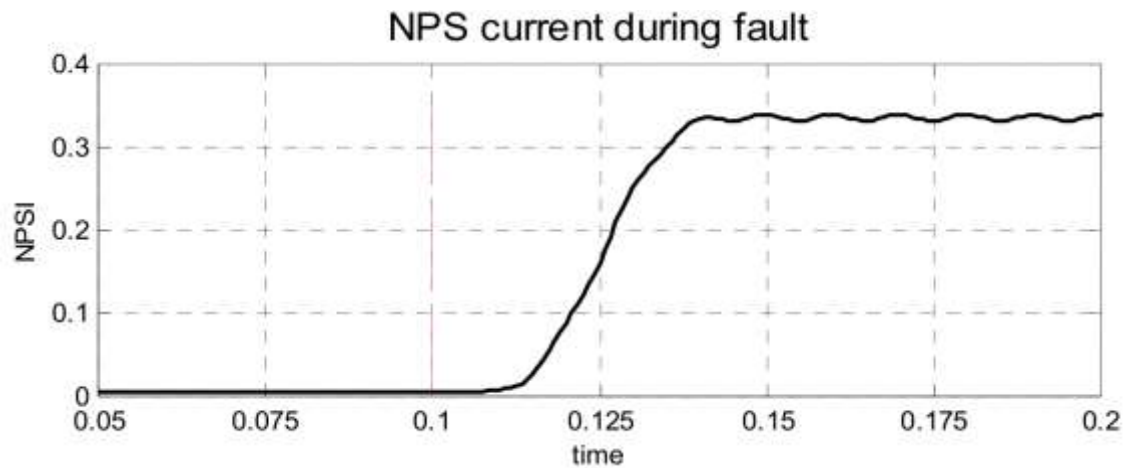


Figure 7. Loss of Two Phases of the Load

An investigation was conducted to determine the reasons for the fluctuations in the recorded negative phase sequence component following the loss of two load phases, as illustrated in Figure 7. The method employed for tracking power system frequency to synchronize the sample with the power system signal pattern encountered difficulties in this regard. The effectiveness of the tracking method may be compromised if it incorporates excessive filtering and pauses. This issue is particularly relevant in applications involving small to medium-sized generation, as such configurations can lead to significant frequency variations following a disturbance.

IV. CONCLUSIONS.

Through the use of a three-phase rotating set of reference phasors as the foundation for a filter that is designed to extract the negative phase sequence from three-phase data, an appealing protection and monitoring method may be developed. The use of a two-cycle Kaiser window results in an efficient filter characteristic and a possible signal extraction time that ranges from ten to forty milliseconds respectively. It is recommended that a delay of thirty to forty milliseconds be included into a relaying application in order to prevent the likelihood of a nuisance tripping occurring as a result of filter transitory actions. This would result in a tripping time that is dependable and falls anywhere between 40 and 80 milliseconds. Together with the accompanying positive and zero phase sequence algorithm, this negative phase sequence extraction technique is capable of being implemented in a protection platform that is based on a DSP processor and uses an adequate sampling rate. This is possible since the platform is based on a numeric microprocessor. In further study, these concepts will be developed in order to offer particular relaying capabilities and to include these algorithms into software that is capable of performing many relay roles.

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