# A Little Modification in Least Cost Method for Unbalanced Transportation Problem 

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#### Abstract

Operation research is a branch of mathematics whereas Transportation problem is sub-branch of operation research. Transportation Problem can be solved by many methods such as North West Corner Rule (NWC), Least Cost Method (LCM), and Vogel's Approximation Method (VAM) etc. In this paper we are discussing Least Cost Method for unbalanced transportation problem and way of allocations to dummy row/column. We have made a few modifications in our proposed algorithm which gives minimum cost or nearer to optimal cost.


Terms used: Transportation Problem, LCM, VAM, unbalanced transportation problem, Feasible Solution, Optimal Solution.

Existing Methods: Initially we mention that there are several algorithms exists for finding feasible solution of Transportation Problem such as North West Corner Rule (NWC), Least Cost Method (LCM), Vogel's Approximation Method (VAM) etc.

## Existing algorithm of LCM is given below:

Step-1: Find the minimum/smallest cost element in the cost matrix.

Step-2: Allocate to the least/smallest element as per demand and supply. Allocate min (Supply, Demand).
Step-3: If minimum cost appear in two or more times in a cost matrix allocate as much as possible to the variable with the least cost in the selected row or column.

Step-4: Give the supply and demand and cross the satisfied row or column.
Step-5: For second allocation find the next least element and allocate according demand and supply.
Step-6: Continue the process until all demands and supply exhausted .
Step-7: For total cost multiply allocations to initial costs and add
This existing method has confusion for a unbalanced transportation problem regarding allocation to zero in dummy row. So I have suggested a method for unbalanced problem which will remove the discrepancy of allocation to zero.

Proposed: LCM method for Unbalanced Transportation Problem.

Unbalanced Transportation Problem: The transportation problem in which sum of demand is not equal to sum of supply is called unbalanced transportation problem. To solve UBTP first we make it balance by adding Dummy row/Column having cost zero.

Step-1: If the transportation is unbalanced add dummy Row/column with zero cost.
(i) If sum of demand is less than sum of supply then add Dummy column with Demand=(Sum of supplySum of demand)
(ii) If sum of supply is less than sum of demand then add Dummy row with Supply=(Sum of demand-Sum of supply)

Step-2: Now in balanced transportation problem find the minimum/smallest element.
Step-3: In all zeros of dummy row/column to which zero we have to allocate is confusion
Step-4: Firstly allocate that zero which is in the last row \& in RHS of table which will
break the tie and will give least cost as compared with other than last row zero
allocations.
Step-5: Give the supply and demand and cross the satisfied row or column.
Step-6: For second allocation find the next least element and allocate according demand and supply
Step-7: Continue the process until all demands and supply exhausted.
Step-8: For total cost multiply allocations to initial costs and add.

We are discussing here some examples for verification of method:-

## Examples of unbalanced transportation problem

## Example 1: Solve the following Transportation problem by LCM.

| Source | Destinations |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Supply |  |  |  |  |  |
|  | F1 | F2 | F3 | F4 | F5 |  |
| M1 | 5 | 4 | 8 | 6 | $\mathbf{5}$ | $\mathbf{6 0 0}$ |
| M2 | 4 | 5 | 4 | 3 | $\mathbf{2}$ | $\mathbf{4 0 0}$ |
| M3 | 3 | 6 | 5 | 8 | $\mathbf{4}$ | $\mathbf{1 0 0 0}$ |
| Demand | $\mathbf{4 5}$ | $\mathbf{4 0 0}$ | $\mathbf{2 0 0}$ | $\mathbf{2 5}$ | $\mathbf{3 0 0}$ |  |

Solution: Since the given problem is unbalanced Transportation Problem so we will add dummy row to make it balance.

| Source | Destinations |  |  |  |  |  | Dumm |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | F1 | F2 | F3 | F4 | F5 | y |  |
| M1 | 5 | 4 | 8 | 6 | $\mathbf{5}$ | $\mathbf{0}$ | $\mathbf{6 0 0}$ |
| M2 | 4 | 5 | 4 | 3 | $\mathbf{2}$ | $\mathbf{0}$ | $\mathbf{4 0 0}$ |
| M3 | 3 | 6 | 5 | 8 | $\mathbf{4}$ | $\mathbf{0}$ | $\mathbf{1 0 0 0}$ |
| Demand | $\mathbf{4 5}$ | $\mathbf{4 0 0}$ | $\mathbf{2 0 0}$ | $\mathbf{2 5}$ | 300 | 400 | $2000 / 2000$ |

Method 1
In table 1 we are allocating to zero of first row as minimum element

Table 1

| Source | Destinations |  |  |  | F5 | Dummy | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | F1 | F2 | F3 | F4 |  |  |  |
| M1 | 5 | $4{ }^{200}$ | 8 | 6 | 5 | $0^{400}$ | 600 |
| M2 | 4 | 5 | 4 | $3{ }^{100}$ | $2^{300}$ | 0 | 400 |
| M3 | $3^{450}$ | $6^{200}$ | 280 | $8^{\text {100 }}$ | 4 | 0 | 1000 |
| Demand | 450 | ${ }_{0}^{40}$ | 200 | ${ }_{0}^{25}$ | 300 |  |  |

Total cost $=4 \times 200+0 \times 400+3 \times 100+2 \times 300+6 \times 200+5 \times 200+8 \times 150+3 \times 450=\mathbf{6 4 5 0}$

In table 2 we are allocating to zero of second row as minimum element

Table 2

| Source | Destinations |  |  |  |  | Dummy | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | F1 | F2 | F3 | F4 | F5 |  | $\mathbf{0}$ |
| M1 | 5 | $4^{400}$ | 8 | $6_{0}^{20}$ | $\mathbf{5}$ | $\mathbf{0}$ | $\mathbf{6 0 0}$ |
| M2 | 4 | 5 | 4 | 3 | $\mathbf{2}$ | $\mathbf{0}^{400}$ | $\mathbf{4 0 0}$ |
| M3 | $3^{450}$ | 6 | $5^{200}$ | $8^{30}$ | $\mathbf{4}^{300}$ | $\mathbf{0}$ | $\mathbf{1 0 0 0}$ |
| Demand | $\mathbf{4 5}$ | $\mathbf{4 0 0}$ | $\mathbf{2 0 0}$ | $\mathbf{2 5}$ | 300 |  |  |

Total cost $=4 \times 400+0 \times 400+4 \times 300+6 \times 200+5 \times 200+8 \times 50+3 \times 450=6750$

In table 3 we are allocating to zero of third row as minimum element
Table 3

| Source | Destinations |  |  |  |  |  | Dummy |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  | F1 | F2 | F3 | F4 | F5 |  |  |
| M1 | 5 | $4^{400}$ | $8^{50}$ | $6_{0}^{15}$ | $\mathbf{5}$ | $\mathbf{0}$ | $\mathbf{6 0 0}$ |
| M2 | 4 | 5 | 4 | $3^{100}$ | $\mathbf{2}^{300}$ | $\mathbf{0}$ | $\mathbf{4 0 0}$ |
| M3 | $3^{450}$ | 6 | $5^{150}$ | 8 | $\mathbf{4}$ | $\mathbf{0}^{400}$ | $\mathbf{1 0 0 0}$ |
| Demand | $\mathbf{4 5}$ | $\mathbf{4 0 0}$ | $\mathbf{2 0 0}$ | $\mathbf{2 5}$ | 300 |  |  |

Total cost : $4 \times 400+8 \times 50+6 \times 150+3 \times 100+2 \times 300+3 \times 450+5 \times 150+0 \times 400=\mathbf{5 9 0 0}$

Example 2: Solve transportation problem by LCM

| WAREHOUSE |  | $\mathbf{B}$ | $\mathbf{C}$ | Supply |
| :---: | :--- | :--- | :--- | :--- |
| $\mathbf{X}$ | 11 | 21 | 16 | 14 |
| $\mathbf{Y}$ | 7 | 17 | 13 | 26 |
| $\mathbf{Z}$ | 11 | 23 | 21 | 36 |
| Demand | 18 | 28 | 25 | $71 / 76$ |

## Solution:

Since the given problem is unbalanced Transportation Problem so we will add dummy row to make it balance.

## Table 1

| WAREHOUSE |  | $\mathbf{B}$ | $\mathbf{C}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{X}$ | 11 | 21 | $16^{9}$ | $0^{5}$ | 14 |
| $\mathbf{Y}$ | $7^{18}$ | 17 | $13^{8}$ | 0 | 26 |
| $\mathbf{Z}$ | 11 | $23^{28}$ | $21^{8}$ | 0 | 36 |
| $\mathbf{D e m a n d}$ | 18 | 28 | 25 | 05 | $76 / 76$ |

Total cost $=7 \times 18+23 \times 28+16 \times 9+13 \times 8+21 \times 8+0 \times 5=\mathbf{1 1 8 6}$

Table 2

| DESTINATION <br> WAREHOUSE | A | $\bar{B}$ | C | DUMMY | Supply |
| :---: | :---: | :---: | :---: | :---: | :---: |
| X | 11 | 21 | $16^{14}$ | 0 | 14 |
| Y | $7^{18}$ | 17 | $13{ }^{3}$ | $0{ }^{5}$ | 26 |
| Z | 11 | $23{ }^{28}$ | $21{ }^{8}$ | 0 | 36 |
| Demand | 18 | 28 | 25 | 05 | 76/76 |

Total cost $=7 \times 18+23 \times 28+16 \times 14+13 \times 3+21 \times 8+0 \times 5=\mathbf{1 2 0 1}$

Table 3

| Destination | $\mathbf{A}$ | $\mathbf{B}$ | $\mathbf{C}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{waremouse}^{\text {warehin }}$ |  |  |  | Supply |  |
| $\mathbf{X}$ | $\mathbf{1 1}$ | $\mathbf{2 1}$ | $\mathbf{1 6}^{\mathbf{1 4}}$ | $\mathbf{0}$ | $\mathbf{1 4}$ |
| $\mathbf{Y}$ | $\mathbf{7}^{\mathbf{1 8}}$ | $\mathbf{1 7}^{\mathbf{8}}$ | $\mathbf{1 3}$ | $\mathbf{0}$ | $\mathbf{2 6}$ |


| Z | $\mathbf{1 1}$ | $\mathbf{2 3}^{20}$ | $21^{11}$ | $0^{\mathbf{1 0}}$ | 36 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Demand | 18 | 28 | 25 | 05 | $76 / 76$ |

Total cost $=7 \times 18+17 \times 8+23 \times 20+16 \times 14+21 \times 11+0 \times 5=1177$

Observation: in above Example-1 least cost method gives the feasible solution

| Table 1 | $\mathbf{6 4 5 0}$ | 5600 | Assigned zero of first <br> row |
| :---: | :---: | :---: | :---: | :---: |
| Table 2 | $\mathbf{6 7 5 0}$ | 5600 | Assigned zero of <br> second row |
| Table 3 | $\mathbf{5 9 0 0}$ | 5600 | Assigned zero of third <br> row |
| In Example 2 | 1119 | Assigned zero of first <br> row |  |
| Table 1 | $\mathbf{1 1 8 6}$ | 1119 | Assigned zero of <br> second row |
| Table 2 | $\mathbf{1 2 0 1}$ | 1119 | Assigned zero of third <br> row |
| Table 3 | $\mathbf{1 1 7 7}$ |  |  |

Result Analysis: In above two examples we observed that by assigning to zero of last row it provides the better solution than other zeros (except the zero of last row). We also tried it for another unbalanced problems and found the same observation.

Conclusion: In this paper we observed that unbalanced transportation problem solved by Least Cost Method gives the minimum cost when zero in the last row allocated first. The solution/cost given by this method is not optimal but it removes the discrepancy of allocation of zeros in dummy row. Allocations made by this criterion may give minimum solution as compared with another but not guaranteed for all problems of different kinds.

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